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Supersymmetry: Model variants, neutrino physics, LHC phenomenology & dark matter

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Introduction

MSSM: The Minimal Supersymmetric Standard Model

R-parity conserving model

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R-parity conserving model

R-parity
is a Z^2
symmetry



SUSY particles appear in even numbers. As a result the lightest SUSY particle, LSP, can not decay

MSSM: The Minimal Supersymmetric Standard Model

R-parity conserving model



The LSP is a good dark matter candidate

Neutralino, sneutrino (experimentally excluded in MSSM), gravitino (gravitino problem)

Problems:

μ -problem: It is necessary to include a

SUSY conserving mass, but can not be at the natural scales, GUT (or Planck), in order to properly break EW symmetry spontaneously

Massless Neutrinos: To solve this

GUT scale see-saw can be used

Regarding the superpotential:

$$W_0 = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c \right)$$

Giudice Masiero mechanism can be used to solve the mu-problem

$$W_0 + \mu H_1 H_2$$

MSSM

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NMSSM solves the μ -problem adding a new superfield

$$W_0 + \lambda S H_1 H_2 + k S S S$$

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$$+ Y_\nu H_2 L \nu^c + M_M \nu^c \nu^c$$

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In this case we basically have at low energy the
MSSM or NMSSM
(same philosophy as in the SM)

$$W_0 = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c \right)$$

Many possibilities to extend the MSSM and NMSSM including neutrino physics with R-parity conservation

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Many possibilities to extend the MSSM and NMSSM including neutrino physics with R-parity conservation

In all R-parity conserving extensions of NMSSM and MSSM

Two trivial consequences in particular region of parameter space:

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Many possibilities to extend the MSSM and NMSSM including neutrino physics with R-parity conservation

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Two trivial consequences in particular region of parameter space:

- **Extra matter implies extra possible LSP (a may be dark matter candidate)**
(The viability of the dark matter candidate must be proved)

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Many possibilities to extend the MSSM and NMSSM including neutrino physics with R-parity conservation

In all R-parity conserving extensions of NMSSM and MSSM

Two trivial consequences in particular region of parameter space:

- **Extra matter implies extra possible LSP (a may be dark matter candidate)**
(The viability of the dark matter candidate must be proved)
- **More complicated Lagrangian may imply possibility of spontaneous R-parity breaking**
(To find this kind of solutions it is not trivial at all)

$$W_0 = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c \right)$$

Example I: MSSM + Dirac Neutrinos

$$W_0 + \mu H_1 H_2 + Y_\nu H_2 L \nu^c$$

Vaccua not complicated enough to open the possibility of spontaneous R-parity breaking

Enhanced sneutrino sector giving the sneutrino (with significant right-handed composition) as a viable **dark matter** candidate (Chiara Arina et al. 2006 and more authors and papers ...)

$$W_0 = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c \right)$$

Example II:

The NMSSM plus Right-handed neutrinos with dynamically generated see-saw

$$\underbrace{W_0 + \lambda S H_1 H_2 + k S S S}_{\text{NMSSM}} + \underbrace{Y_\nu H_2 L \nu^c + S \nu^c \nu^c}_{\text{Kitano \& Oda, 1999}}$$

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Vacua complicated enough to open the possibility of **spontaneous R-parity breaking** (K.O. 1999)

Right-handed sneutrino is a viable possible **dark matter** candidate with this superpotential (Cerdeño, Muñoz & Seto 2008 and more papers ...)

Neutrino physics (including loops) has been studied by Das & Roy, 2010, and others

Similar Superpotential was also introduced by Garbrecht & Pilaftis, 2006. Right-handed sneutrino as dark matter was analysed in 2008 in this context by Deppisch & Pilaftis.

$$W_0 = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c \right)$$

Many possibilities to extend the MSSM and NMSSM including neutrino physics with R-parity conservation

GUT scale Majorana mass, Inverse see-saw, Type II or Type III see-saw, Dynamically generated see-saw, and more, and more, possibilities

**Remember -> In all R-parity conserving extensions of NMSSM and MSSM
Two trivial consequences in particular region of parameter space:**

- **Extra matter implies extra possible LSP (a may be dark matter candidate)**
(The viability of the dark matter candidate must be proved)
- **More complicated Lagrangian may imply possibility of spontaneous R-parity breaking**
(To find this kind of solutions it is not trivial at all)

R-parity conserving models are very interesting

However

We do not need to add a new extra singlet superfield as in the NMSSM to solve the μ -problem •••

We can use right handed neutrino superfield(s) to solve the μ -problem and to give mass to the neutrinos

The μ from ν Supersymmetric Standard Model : The $\mu\nu$ SSM

SUSY model with minimal natural content of matter

Right-handed neutrino superfield(s) giving mass to the neutrinos

and solving the μ -problem of the MSSM

As a consequence: R-parity is explicitly broken

Gravitino is the superpartner of the graviton. Present in a very minimal way in supersymmetry

Gravitino do not need an exact symmetry to be protected to decay; interacts only gravitationally

We have a minimal natural
framework

An alternative to the MSSM
(and R-parity conserving extensions)

SUGRA (local SUSY)

$(G_{\mu\nu}, \Psi_{\mu})$
(graviton, gravitino)

$M_{\text{Planck}} \sim 10^{16} \text{ TeV}$
(Non Renormalizable)

Tree level amplitudes

Dark Matter candidate

SUSY

$\mu\nu\text{SSM}$

$M_{\text{SUSY}} \sim 1 \text{ TeV}$

(Renormalizable)

Similar as in a Fermi theory where

$$G_F \sim 1/M_w^2$$

The Model

SUSY renormalizable model: $\mu\nu$ SSM

$$W = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c + Y_\nu^{ij} \hat{H}_2^b \hat{L}_i^a \hat{\nu}_j^c \right) \\ - \epsilon_{ab} \lambda^i \hat{\nu}_i^c \hat{H}_1^a \hat{H}_2^b + \frac{1}{3} \kappa^{ijk} \hat{\nu}_i^c \hat{\nu}_j^c \hat{\nu}_k^c,$$

All known particles + SUSY partners
(including neutrinos physics)

SUSY renormalizable model: $\mu\nu$ SSM

$$W = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c + Y_\nu^{ij} \hat{H}_2^b \hat{L}_i^a \hat{\nu}_j^c \right) \\ - \epsilon_{ab} \lambda^i \hat{\nu}_i^c \hat{H}_1^a \hat{H}_2^b + \frac{1}{3} \kappa^{ijk} \hat{\nu}_i^c \hat{\nu}_j^c \hat{\nu}_k^c,$$

Only dimensionless parameters in
the superpotential

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Only dimensionless parameters in
the superpotential

Possible interpretation: particles are in principle massless but the spontaneous breaking of supersymmetry in the SUGRA theory generates the soft terms (breaking explicitly global SUSY)

SUSY renormalizable model: $\mu\nu$ SSM

Soft Terms

Are given by SUGRA

$$\begin{aligned} -\mathcal{L}_{\text{soft}} &= m_{H_1}^2 H_1^{a*} H_1^a + m_{H_2}^2 H_2^{a*} H_2^a + (m_{\tilde{\nu}^c}^2)^{ij} \tilde{\nu}_i^{c*} \tilde{\nu}_j^c + \dots \\ &+ \left[\epsilon_{ab} (A_\nu Y_\nu)^{ij} H_2^b \tilde{L}_i^a \tilde{\nu}_j^c + \dots + \frac{1}{3} (A_\kappa \kappa)^{ijk} \tilde{\nu}_i^c \tilde{\nu}_j^c \tilde{\nu}_k^c + \text{H.c.} \right] \\ &- \frac{1}{2} \left(M_3 \tilde{\lambda}_3 \tilde{\lambda}_3 + M_2 \tilde{\lambda}_2 \tilde{\lambda}_2 + M_1 \tilde{\lambda}_1 \tilde{\lambda}_1 + \text{H.c.} \right). \end{aligned}$$

The SUSY breaking scale, only source of spontaneous gauge breaking.

THE ONLY SCALE

SUSY renormalizable model: $\mu\nu$ SSM

$$W = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c + Y_\nu^{ij} \hat{H}_2^b \hat{L}_i^a \hat{\nu}_j^c \right) \\ - \epsilon_{ab} \lambda^i \hat{\nu}_i^c \hat{H}_1^a \hat{H}_2^b + \frac{1}{3} \kappa^{ijk} \hat{\nu}_i^c \hat{\nu}_j^c \hat{\nu}_k^c,$$

R-parity is not a symmetry of the model

SUSY renormalizable model: $\mu\nu$ SSM

$$W = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c + Y_\nu^{ij} \hat{H}_2^b \hat{L}_i^a \hat{\nu}_j^c \right) \\ - \epsilon_{ab} \lambda^i \hat{\nu}_i^c \hat{H}_1^a \hat{H}_2^b + \frac{1}{3} \kappa^{ijk} \hat{\nu}_i^c \hat{\nu}_j^c \hat{\nu}_k^c,$$

$$Y_\nu^{ij} = 0 \Rightarrow \text{R-parity is conserved}$$

Possible interpretation:

R-parity is not an exact symmetry giving the LSP as DM, is an approximative symmetry protecting neutrino masses to be small

SUSY renormalizable model: $\mu\nu$ SSM

$$W = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c + Y_\nu^{ij} \hat{H}_2^b \hat{L}_i^a \hat{\nu}_j^c \right) \\ - \epsilon_{ab} \lambda^i \hat{\nu}_i^c \hat{H}_1^a \hat{H}_2^b + \frac{1}{3} \kappa^{ijk} \hat{\nu}_i^c \hat{\nu}_j^c \hat{\nu}_k^c,$$

Once the electroweak symmetry is spontaneously broken, the neutral scalars develop in general the following VEVs:

$$\langle H_1^0 \rangle = v_1, \quad \langle H_2^0 \rangle = v_2, \quad \langle \tilde{\nu}_i^c \rangle = \nu_i^c$$

$$\langle \tilde{\nu}_i \rangle = \nu_i$$

Goes to zero when $Y_\nu^{ij} \longrightarrow 0$

SUSY renormalizable model: $\mu\nu$ SSM

$$\begin{aligned}
 W = & \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c + \underbrace{Y_\nu^{ij} \hat{H}_2^b \hat{L}_i^a \hat{\nu}_j^c}_{\text{Effective Dirac Mass}} \right) \\
 & - \epsilon_{ab} \underbrace{\lambda^i \hat{\nu}_i^c \hat{H}_1^a \hat{H}_2^b}_{\text{Effective } \mu\text{-term}} + \frac{1}{3} \underbrace{\kappa^{ijk} \hat{\nu}_i^c \hat{\nu}_j^c \hat{\nu}_k^c}_{\text{Effective Majorana Mass}},
 \end{aligned}$$

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Effective Bilinear term

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 \end{aligned}$$

Effective Bilinear term

Effective bilinear term \Rightarrow One right-handed neutrino is enough to reproduce neutrino physics (through loops) but three is natural

SUSY renormalizable model: $\mu\nu$ SSM

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Effective Bilinear term

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MSSM + bilinear R-parity breaking term ($\epsilon H_2 L$) is a very well known model (the μ -problem is augmented respect to the MSSM)

Hall, Suzuki, 1984; Lee, 1984; Dawson, 1985; ...

Phenomenology

R-parity conserving models (MSSM, NMSSM, etc.):

Lightest Supersymmetric particle (LSP) : Dark Matter candidate
(neutralino, sneutrino, gravitino, ...)

Collider signature \rightarrow missing energy (Collider detectors are of order meter, a particle with lifetime bigger than 10^{-8} s can escape the detector, dark matter experiments are necessary)

$\mu\nu$ S**SM** (minimal natural content of matter) :

R-parity breaking model:

Gravitino is a possible **dark matter** candidate: Indirect detection possible (more DM candidates, as for instance axion and axino, are possible)

Neutrino physics: very easy to reproduce neutrino physics

Sneutrinos are part of the **Higgs sector:** Rich Higgs sector

Collider signature: Multileptons, multijets, displaced vertices

(R-parity breaking related with neutrino physics. We have a long life particle. missing energy if decays outside the collider or in the form of neutrinos)

- **Neutrinos mix with neutralino (10 X 10)**
3 light neutrinos (mainly neutrinos left-handed)
+ 7 mainly neutralinos (including neutrinos right-handed)

- **Neutral Higgs mix with sneutrinos (8 X 8)**
8 CP even Higgses (5 + 3 mainly sneutrinos left-handed)
7 CP odd Higgses (4 + 3 mainly sneutrinos left-handed)

The Neutralino-Neutrino mass matrix is:

$$\mathcal{M}_n = \begin{pmatrix} M & m \\ m^T & 0_{3 \times 3} \end{pmatrix},$$

$$M = \begin{pmatrix} M_1 & 0 & -Av_d & Av_u & 0 & 0 & 0 \\ 0 & M_2 & Bv_d & -Bv_u & 0 & 0 & 0 \\ -Av_d & Bv_d & 0 & -\lambda_i \nu_i^c & -\lambda_1 v_u & -\lambda_2 v_u & -\lambda_3 v_u \\ Av_u & -Bv_u & -\lambda_i \nu_i^c & 0 & -\lambda_1 v_d + Y_{\nu_{i1}} \nu_i & -\lambda_2 v_d + Y_{\nu_{i2}} \nu_i & -\lambda_3 v_d + Y_{\nu_{i3}} \nu_i \\ 0 & 0 & -\lambda_1 v_u & -\lambda_1 v_d + Y_{\nu_{i1}} \nu_i & 2\kappa_{11j} \nu_j^c & 2\kappa_{12j} \nu_j^c & 2\kappa_{13j} \nu_j^c \\ 0 & 0 & -\lambda_2 v_u & -\lambda_2 v_d + Y_{\nu_{i2}} \nu_i & 2\kappa_{21j} \nu_j^c & 2\kappa_{22j} \nu_j^c & 2\kappa_{23j} \nu_j^c \\ 0 & 0 & -\lambda_3 v_u & -\lambda_3 v_d + Y_{\nu_{i3}} \nu_i & 2\kappa_{31j} \nu_j^c & 2\kappa_{32j} \nu_j^c & 2\kappa_{33j} \nu_j^c \end{pmatrix},$$

where $A = \frac{G}{\sqrt{2}} \sin \theta_W$, $B = \frac{G}{\sqrt{2}} \cos \theta_W$, and

$$m^T = \begin{pmatrix} -\frac{g_1}{\sqrt{2}} \nu_1 & \frac{g_2}{\sqrt{2}} \nu_1 & 0 & Y_{\nu_{1i}} \nu_i^c & Y_{\nu_{11}} v_u & Y_{\nu_{12}} v_u & Y_{\nu_{13}} v_u \\ -\frac{g_1}{\sqrt{2}} \nu_2 & \frac{g_2}{\sqrt{2}} \nu_2 & 0 & Y_{\nu_{2i}} \nu_i^c & Y_{\nu_{21}} v_u & Y_{\nu_{22}} v_u & Y_{\nu_{23}} v_u \\ -\frac{g_1}{\sqrt{2}} \nu_3 & \frac{g_2}{\sqrt{2}} \nu_3 & 0 & Y_{\nu_{3i}} \nu_i^c & Y_{\nu_{31}} v_u & Y_{\nu_{32}} v_u & Y_{\nu_{33}} v_u \end{pmatrix}$$

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$$M = \begin{pmatrix} M_1 & 0 & -Av_d & Av_u & 0 & 0 & 0 \\ 0 & M_2 & Bv_d & -Bv_u & 0 & 0 & 0 \\ -Av_d & Bv_d & 0 & -\lambda_i \nu_i^c & -\lambda_1 v_u & -\lambda_2 v_u & -\lambda_3 v_u \\ Av_u & -Bv_u & -\lambda_i \nu_i^c & 0 & -\lambda_1 v_d + Y_{\nu_{i1}} \nu_i & -\lambda_2 v_d + Y_{\nu_{i2}} \nu_i & -\lambda_3 v_d + Y_{\nu_{i3}} \nu_i \\ 0 & 0 & -\lambda_1 v_u & -\lambda_1 v_d + Y_{\nu_{i1}} \nu_i & 2\kappa_{11j} \nu_j^c & 2\kappa_{12j} \nu_j^c & 2\kappa_{13j} \nu_j^c \\ 0 & 0 & -\lambda_2 v_u & -\lambda_2 v_d + Y_{\nu_{i2}} \nu_i & 2\kappa_{21j} \nu_j^c & 2\kappa_{22j} \nu_j^c & 2\kappa_{23j} \nu_j^c \\ 0 & 0 & -\lambda_3 v_u & -\lambda_3 v_d + Y_{\nu_{i3}} \nu_i & 2\kappa_{31j} \nu_j^c & 2\kappa_{32j} \nu_j^c & 2\kappa_{33j} \nu_j^c \end{pmatrix},$$

where $A = \frac{G}{\sqrt{2}} \sin \theta_W$, $B = \frac{G}{\sqrt{2}} \cos \theta_W$, and

$$m^T = \begin{pmatrix} -\frac{g_1}{\sqrt{2}} \nu_1 & \frac{g_2}{\sqrt{2}} \nu_1 & 0 & Y_{\nu_{1i}} \nu_i^c & Y_{\nu_{11}} v_u & Y_{\nu_{12}} v_u & Y_{\nu_{13}} v_u \\ -\frac{g_1}{\sqrt{2}} \nu_2 & \frac{g_2}{\sqrt{2}} \nu_2 & 0 & Y_{\nu_{2i}} \nu_i^c & Y_{\nu_{21}} v_u & Y_{\nu_{22}} v_u & Y_{\nu_{23}} v_u \\ -\frac{g_1}{\sqrt{2}} \nu_3 & \frac{g_2}{\sqrt{2}} \nu_3 & 0 & Y_{\nu_{3i}} \nu_i^c & Y_{\nu_{31}} v_u & Y_{\nu_{32}} v_u & Y_{\nu_{33}} v_u \end{pmatrix}$$

The Neutralino-Neutrino mass matrix is:

$$\mathcal{M}_n = \begin{pmatrix} M & m \\ m^T & 0_{3 \times 3} \end{pmatrix},$$

$$M = \begin{pmatrix} M_1 & 0 & -Av_d & Av_u & 0 & 0 & 0 \\ 0 & M_2 & Bv_d & -Bv_u & 0 & 0 & 0 \\ -Av_d & Bv_d & 0 & -\lambda_i \nu_i^c & -\lambda_1 v_u & -\lambda_2 v_u & -\lambda_3 v_u \\ Av_u & -Bv_u & -\lambda_i \nu_i^c & 0 & -\lambda_1 v_d + Y_{\nu_{i1}} \nu_i & -\lambda_2 v_d + Y_{\nu_{i2}} \nu_i & -\lambda_3 v_d + Y_{\nu_{i3}} \nu_i \\ 0 & 0 & -\lambda_1 v_u & -\lambda_1 v_d + Y_{\nu_{i1}} \nu_i & 2\kappa_{11j} \nu_j^c & 2\kappa_{12j} \nu_j^c & 2\kappa_{13j} \nu_j^c \\ 0 & 0 & -\lambda_2 v_u & -\lambda_2 v_d + Y_{\nu_{i2}} \nu_i & 2\kappa_{21j} \nu_j^c & 2\kappa_{22j} \nu_j^c & 2\kappa_{23j} \nu_j^c \\ 0 & 0 & -\lambda_3 v_u & -\lambda_3 v_d + Y_{\nu_{i3}} \nu_i & 2\kappa_{31j} \nu_j^c & 2\kappa_{32j} \nu_j^c & 2\kappa_{33j} \nu_j^c \end{pmatrix},$$

where $A = \frac{G}{\sqrt{2}} \sin \theta_W$, $B = \frac{G}{\sqrt{2}} \cos \theta_W$, and

$$m^T = \begin{pmatrix} -\frac{g_1}{\sqrt{2}} \nu_1 & \frac{g_2}{\sqrt{2}} \nu_1 & 0 & Y_{\nu_{1i}} \nu_i^c & Y_{\nu_{11}} v_u & Y_{\nu_{12}} v_u & Y_{\nu_{13}} v_u \\ -\frac{g_1}{\sqrt{2}} \nu_2 & \frac{g_2}{\sqrt{2}} \nu_2 & 0 & Y_{\nu_{2i}} \nu_i^c & Y_{\nu_{21}} v_u & Y_{\nu_{22}} v_u & Y_{\nu_{23}} v_u \\ -\frac{g_1}{\sqrt{2}} \nu_3 & \frac{g_2}{\sqrt{2}} \nu_3 & 0 & Y_{\nu_{3i}} \nu_i^c & Y_{\nu_{31}} v_u & Y_{\nu_{32}} v_u & Y_{\nu_{33}} v_u \end{pmatrix}$$

EW see-saw mechanism

In first approximation the light neutrinos mass matrix is:

$$M_\nu = m^T M^{-1} m$$

With neutrino masses of order $10^{-2} \text{ eV} = 10^{-11} \text{ GeV} \Rightarrow$

$$10^{-11} \text{ GeV} = \frac{Y_\nu^2 (10^2 \text{ GeV})^2}{10^3 \text{ GeV}} \rightarrow Y_\nu \sim 10^{-6}$$

Effective Neutrino mass matrix

$$M_\nu = m^T M^{-1} m$$

Using Diagonal Yukawas for Neutrinos

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$

$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^{c^2} + \lambda v_u v_d)} \left(2\kappa\nu^{c^2} \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right] \quad \frac{1}{M} = \frac{g_1^2}{M_1} + \frac{g_2^2}{M_2}$$

We have neglected all the terms of order $Y_\nu^2 \nu^2$, $Y_\nu^3 \nu$ and $Y_\nu \nu^3$

Some Important limits

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$

$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^{c^2} + \lambda v_u v_d)} \left(2\kappa\nu^{c^2} \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right]$$

Some Important limits

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$
$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^{c^2} + \lambda v_u v_d)} \frac{1}{3\lambda\nu^c} \left(2\kappa\nu^{c^2} \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right]$$

Gaugino see-saw

$$\nu^c \rightarrow \infty \quad (m_{eff|real})_{ij} \simeq -\frac{1}{2M} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$

and $\nu_i \gg \frac{Y_{\nu_i} v_d}{3\lambda}$ $(m_{eff|real})_{ij} \simeq -\frac{\nu_i \nu_j}{2M}$

Some Important limits

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$
$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^{c^2} + \lambda v_u v_d)} \frac{1}{3\lambda\nu^c} \left(2\kappa\nu^{c^2} \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right]$$

Gaugino see-saw

$$\nu^c \rightarrow \infty \quad (m_{eff|real})_{ij} \simeq -\frac{1}{2M} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$

and $v_d \rightarrow 0$ $(m_{eff|real})_{ij} \simeq -\frac{\nu_i \nu_j}{2M}$

Some Important limits

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$
$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^{c^2} + \lambda v_u v_d)} \frac{1}{3\lambda\nu^c} \left(2\kappa\nu^{c^2} \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right]$$

ν_R -Higgsino See-Saw

$$M \rightarrow \infty,$$

Some Important limits

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$
$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^{c^2} + \lambda v_u v_d)} \frac{1}{3\lambda\nu^c} \left(2\kappa\nu^{c^2} \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right]$$

ν_R -Higgsino See-Saw

$$M \rightarrow \infty, \quad (m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij})$$

Some Important limits

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$
$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^{c^2} + \lambda v_u v_d)} \frac{1}{3\lambda\nu^c} \left(2\kappa\nu^{c^2} \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right]$$

A very simple limit

$$v_d \rightarrow 0$$

$$\text{or } \nu_i \gg \frac{Y_{\nu_i} v_d}{3\lambda}$$

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \nu_i \nu_j$$

$$M_{eff} = M \left(1 - \frac{v^4}{12\kappa M \nu^{c^3}} \right)$$

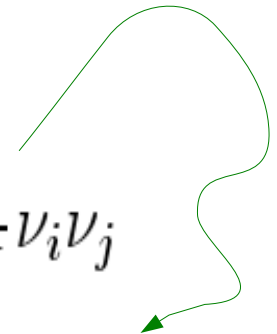
Some Important limits

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$

$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^c + \lambda v_u v_d)} \left(2\kappa\nu^c \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right] \quad \frac{1}{M} = \frac{g_1^2}{M_1} + \frac{g_2^2}{M_2}$$

$$v_d \rightarrow 0$$

$$M_{eff} \approx M$$

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M} \nu_i \nu_j$$


Gaugino see saw

Some Important limits

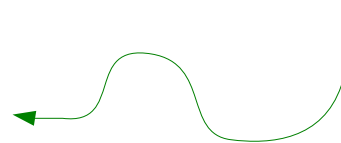
$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$

$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^c + \lambda v_u v_d)} \left(2\kappa\nu^c \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right] \quad \frac{1}{M} = \frac{g_1^2}{M_1} + \frac{g_2^2}{M_2}$$

$$v_d \rightarrow 0 \quad (m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M} \nu_i \nu_j$$

$$M_{eff} \approx M$$

ν_R -Higgsino see saw



Effective Neutrino mass matrix

(Diagonal Yukawas for Neutrinos)

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$

$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^c + \lambda v_u v_d)} \left(2\kappa\nu^c \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right] \quad \frac{1}{M} = \frac{g_1^2}{M_1} + \frac{g_2^2}{M_2}$$

$$v_d \rightarrow 0$$

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M} \nu_i \nu_j$$

$$M_{eff} \approx M$$

ν_R -Higgsino see saw  **Gaugino see saw**

Also with diagonal Yukawas for neutrinos the mixtures could be generated

The ν_μ - ν_τ degenerate case, $Y_{\nu_2} = Y_{\nu_3}$ and $\nu_2 = \nu_3$

$$m_{eff} = \begin{pmatrix} d & c & c \\ c & A & B \\ c & B & A \end{pmatrix}$$

Also with diagonal Yukawas for neutrinos the mixtures could be generated

The ν_μ - ν_τ degenerate case, $Y_{\nu_2} = Y_{\nu_3}$ and $\nu_2 = \nu_3$

$$m_{eff} = \begin{pmatrix} d & c & c \\ c & A & B \\ c & B & A \end{pmatrix}$$

$$\frac{1}{2} \left(A + B - \sqrt{8c^2 + (A + B - d)^2} + d \right), \frac{1}{2} \left(A + B + \sqrt{8c^2 + (A + B - d)^2} + d \right), A - B,$$

$$\left(-\frac{A+B+\sqrt{8c^2+(A+B-d)^2}-d}{2}, c, c \right), \left(\frac{-A-B+\sqrt{8c^2+(A+B-d)^2+d}}{2c}, 1, 1 \right), (0, -1, 1)$$

Also with diagonal Yukawas for neutrinos the mixtures could be generated

The ν_μ - ν_τ degenerate case, $Y_{\nu_2} = Y_{\nu_3}$ and $\nu_2 = \nu_3$

We have ordered the eigenvalues in such a way that it is clear how to obtain the normal hierarchy case

$$m_{eff} = \begin{pmatrix} d & c & c \\ c & A & B \\ c & B & A \end{pmatrix}$$

$$\frac{1}{2} \left(A + B - \sqrt{8c^2 + (A + B - d)^2} + d \right), \frac{1}{2} \left(A + B + \sqrt{8c^2 + (A + B - d)^2} + d \right), A - B,$$

$$\left(-\frac{A+B+\sqrt{8c^2+(A+B-d)^2}-d}{2}, c, c \right), \left(\frac{-A-B+\sqrt{8c^2+(A+B-d)^2}+d}{2c}, 1, 1 \right), (0, -1, 1)$$

Also with diagonal Yukawas for neutrinos the mixtures could be generated

The ν_μ - ν_τ degenerate case, $Y_{\nu_2} = Y_{\nu_3}$ and $\nu_2 = \nu_3$

Bimaximal case

$$m_{eff} = \begin{pmatrix} d & c & c \\ c & A & B \\ c & B & A \end{pmatrix} \quad \sin^2 \theta_{23} = \frac{1}{2}$$

$$\sin^2 \theta_{13} = 0$$

$$\frac{1}{2} \left(A + B - \sqrt{8c^2 + (A + B - d)^2 + d} \right), \frac{1}{2} \left(A + B + \sqrt{8c^2 + (A + B - d)^2 + d} \right), A - B,$$

$$\left(-\frac{A+B+\sqrt{8c^2+(A+B-d)^2-d}}{2}, c, c \right), \left(\frac{-A-B+\sqrt{8c^2+(A+B-d)^2+d}}{2c}, 1, 1 \right), (0, -1, 1)$$

Also with diagonal Yukawas for neutrinos the mixtures could be generated

The ν_μ - ν_τ degenerate case, $Y_{\nu_2} = Y_{\nu_3}$ and $\nu_2 = \nu_3$

Tri-Bimaximal case $m_{eff} = \begin{pmatrix} d & c & c \\ c & A & B \\ c & B & A \end{pmatrix}$ $\sin^2 \theta_{23} = \frac{1}{2}$

$$\sin^2 \theta_{13} = 0$$

$$c = A + B - d \quad \longrightarrow \quad \sin^2 \theta_{12} = 1/3$$

Also with diagonal Yukawas for neutrinos the mixtures could be generated

The ν_μ - ν_τ degenerate case, $Y_{\nu_2} = Y_{\nu_3}$ and $\nu_2 = \nu_3$

Tri-Bimaximal case $m_{eff} = \begin{pmatrix} d & c & c \\ c & A & B \\ c & B & A \end{pmatrix}$ $\sin^2 \theta_{23} = \frac{1}{2}$

$\sin^2 \theta_{13} = 0$

$c = A + B - d \quad \longrightarrow \quad \sin^2 \theta_{12} = 1/3$

Then close to the ν_μ - ν_τ degenerate case, **and** $c \approx A + B - d$

$\sin^2 \theta_{23} \approx \frac{1}{2}$ $\sin^2 \theta_{13} \approx 0$ $\sin^2 \theta_{12} \approx 1/3$

Then is easy to satisfy the latest experimental results !!!

$$7.12 < \Delta m_{sol}^2 / 10^{-5} \text{ eV}^2 < 8.20 , 2.31 < \Delta m_{atm}^2 / 10^{-3} \text{ eV}^2 < 2.74$$

$$0.27 < \sin^2 \theta_{12} < 0.37 , 0.017 < \sin^2 \theta_{13} < 0.033 , 0.36 < \sin^2 \theta_{23} < 0.68.$$

G. L. Fogli *et al.*, *Phys. Rev. D* **78** (2008) 033010 [arXiv:0805.2517 [hep-ph]]; T. Schwetz, M. Tortola and J. W. F. Valle, *New J. Phys.* **13** (2011) 063004 [arXiv:1103.0734 [hep-ph]].

With diagonal Yukawas for neutrinos (and diagonal effective Majorana mass) we can reproduce the experimental mixing angles.

In a sense we have an explanation of :

Why mixtures in Neutrino and quark sectors are so different?

Some papers on neutrino physics in this model:

J. Fidalgo, D. E. L-F, C. Muñoz and R. Ruiz de Austri, *JHEP* **08** (2009) 105

P. Ghosh, P. Dey, B. Mukhopadhyaya and S. Roy, *JHEP* **05** (2010) 087

Electroweak baryogenesis is possible in this model:

Daniel J. H. Chung and Andrew J. Long, *Phys. Rev.* **D81** (2010)

R-parity is broken: LSP is not stable

Neutralino is not a Dark Matter candidate

Also sneutrino (with right-handed component) it is not

But

**Neutralino has an important role in the
SUSY see-saw
(without imposing R parity)**

**Also sneutrinos Right handed as part of the Higgs
has an important role**

Lightest doublet-like Higgs

Tree level bound

On the Lightest Higgs

$$m_h^2 \leq M_Z^2 \left(\cos^2 2\beta + \frac{2\lambda^2 \cos^2 \theta_W}{g_2^2} \sin^2 2\beta \right) \approx M_Z^2 \left(\cos^2 2\beta + 3.62 \lambda^2 \sin^2 2\beta \right)$$

MSSM \nearrow

$$\lambda^2 = \lambda_i \lambda_i$$

Landau pole condition (GUT)



$$\lambda^2 \lesssim (0.7)^2 \quad \lambda \equiv \lambda_i \lesssim 0.7/\sqrt{3} \approx 0.4$$

for $\tan \beta = 2(4)$



$$m_h \lesssim 111(98) \text{ GeV} \quad \text{Tree Level}$$

Pure doublet



$$\lambda_i \rightarrow 0$$

OR

$$A_{\lambda_i} = \frac{2\mu}{\sin 2\beta} - \frac{2}{\lambda_i} \sum_{j,k} \kappa_{ijk} \lambda_j \nu_k^c$$

Easier than in the MSSM to have the lightest doublet-like Higgs with mass around 125 GeV

- If the lightest Higgses are dominated by right-handed sneutrinos the mixing helps to increase the mass of the lightest doublet-like Higgs
- 1 loop contributions increase the lightest doublet-like Higgs mass
- Possible to relax the Landau pole constraint (lower scale). We are not going to use this here.

Gravitino: Good dark matter candidate

Direct detection: Not possible ☹️

Indirect detection: In principle possible !!! 😊

Through the decay

$$\Psi_{3/2} \rightarrow \sum_i \gamma \nu_i$$

Possible signals at LHC

Displaced vertices:

Multi-leptons plus missing energy

P. Ghosh, D. E. L-F, V. Mitsou, C. Muñoz, R. Ruiz de Austri arXiv: 1211.3177

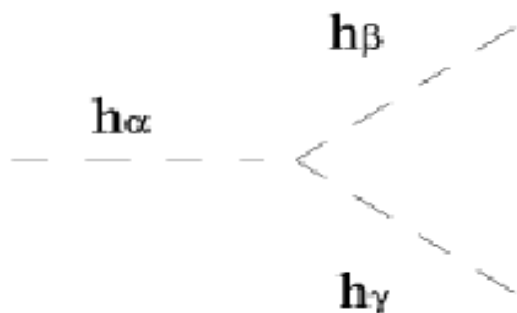
Some More papers on colliders signatures in this model:

A. Bartl, M. Hirsch, A. Vicente, S. Liebler and W. Porod, JHEP **05** (2009) 120

J. Fidalgo, D. E. L-F, C. Muñoz, R. Ruiz de Austri JHEP **10** (2011) 020

P. Bandyopadhyay, P. Ghosh and S. Roy, *Phys. Rev D* **84** (2011)

$h \rightarrow 2$ Standard Model fermions : $h \rightarrow \tau^+ \tau^-$, $h \rightarrow \mu^+ \mu^-$, $h \rightarrow b\bar{b}$, Etc.



$$h_\alpha \rightarrow h_\beta h_\gamma ,$$

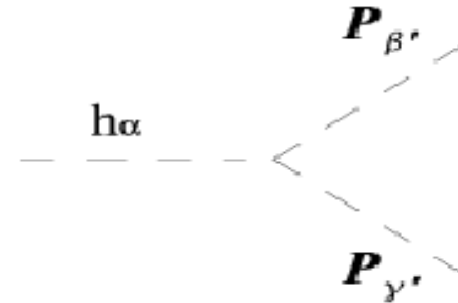
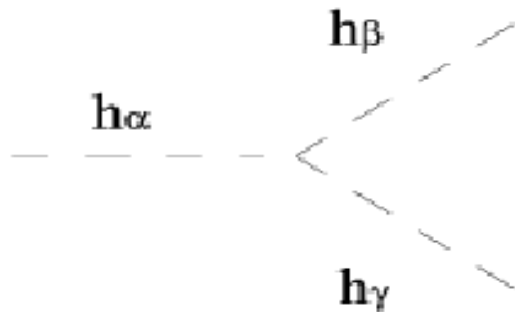
where $\alpha, \beta, \gamma = 1, \dots, 8$ and $\alpha', \beta', \gamma' = 1, \dots, 7$.

For example we have

$$h_3 \rightarrow 2h_2 \rightarrow 4h_1 \rightarrow 8 \text{ Standard Model fermions .}$$

$h \rightarrow 2$ Standard Model fermions : $h \rightarrow \tau^+ \tau^-$, $h \rightarrow \mu^+ \mu^-$, $h \rightarrow b\bar{b}$, Etc.

$P \rightarrow 2$ Standard Model fermions : $P \rightarrow \tau^+ \tau^-$, $P \rightarrow \mu^+ \mu^-$, $P \rightarrow b\bar{b}$, Etc.



$$h_\alpha \rightarrow h_\beta h_\gamma ,$$

$$h_\alpha \rightarrow P_{\beta'} P_{\gamma'} ,$$

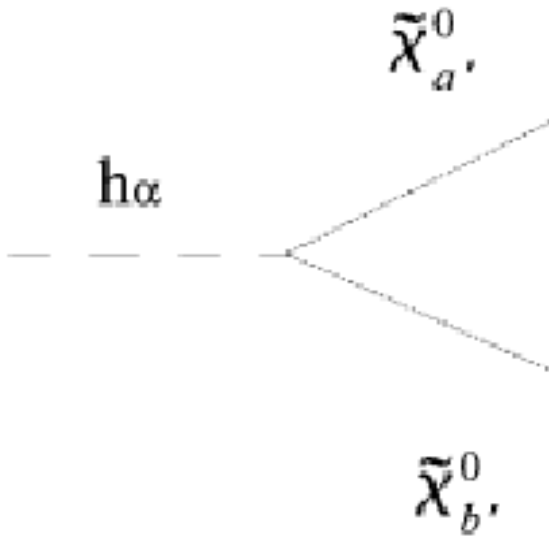
$$P_{\alpha'} \rightarrow P_{\beta'} h_\gamma ,$$

where $\alpha, \beta, \gamma = 1, \dots, 8$ and $\alpha', \beta', \gamma' = 1, \dots, 7$.

For example we have

$$h_3 \rightarrow 2h_2 \rightarrow 4h_1 \rightarrow 8 \text{ Standard Model fermions .}$$

Multileptons and multijets signals

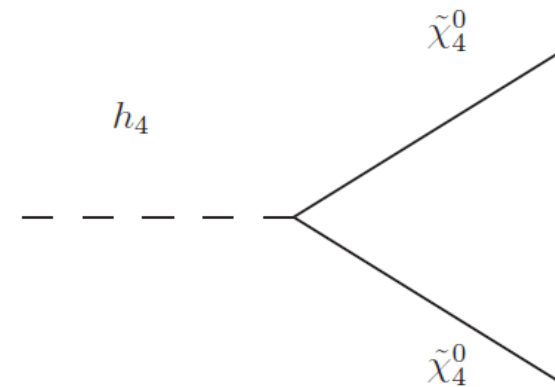


$$h_4 \rightarrow \tilde{\chi}^0 \tilde{\chi}^0 \rightarrow 2P2\nu \rightarrow 2b2\bar{b}2\nu$$

$$h_4 \rightarrow \tilde{\chi}^0 \tilde{\chi}^0 \rightarrow 2P2\nu \rightarrow 2\tau^+ 2\tau^- 2\nu$$

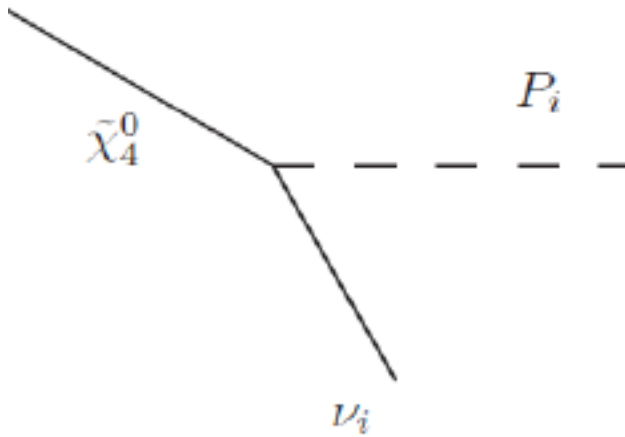
We took three light singlet-like Higgses, the fourth one is doublet-like

$$m_{h_4} \approx 125 \text{ GeV}$$



Displaced vertices signals (or missing energy if $\tilde{\chi}_4^0$ decays outside the detector)

Long life

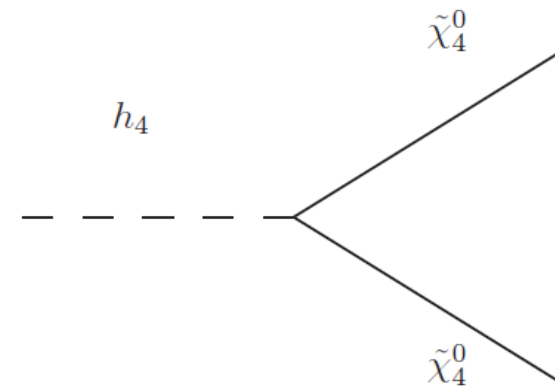


$$h_4 \rightarrow \tilde{\chi}^0 \tilde{\chi}^0 \rightarrow 2P2\nu \rightarrow 2b2\bar{b}2\nu$$

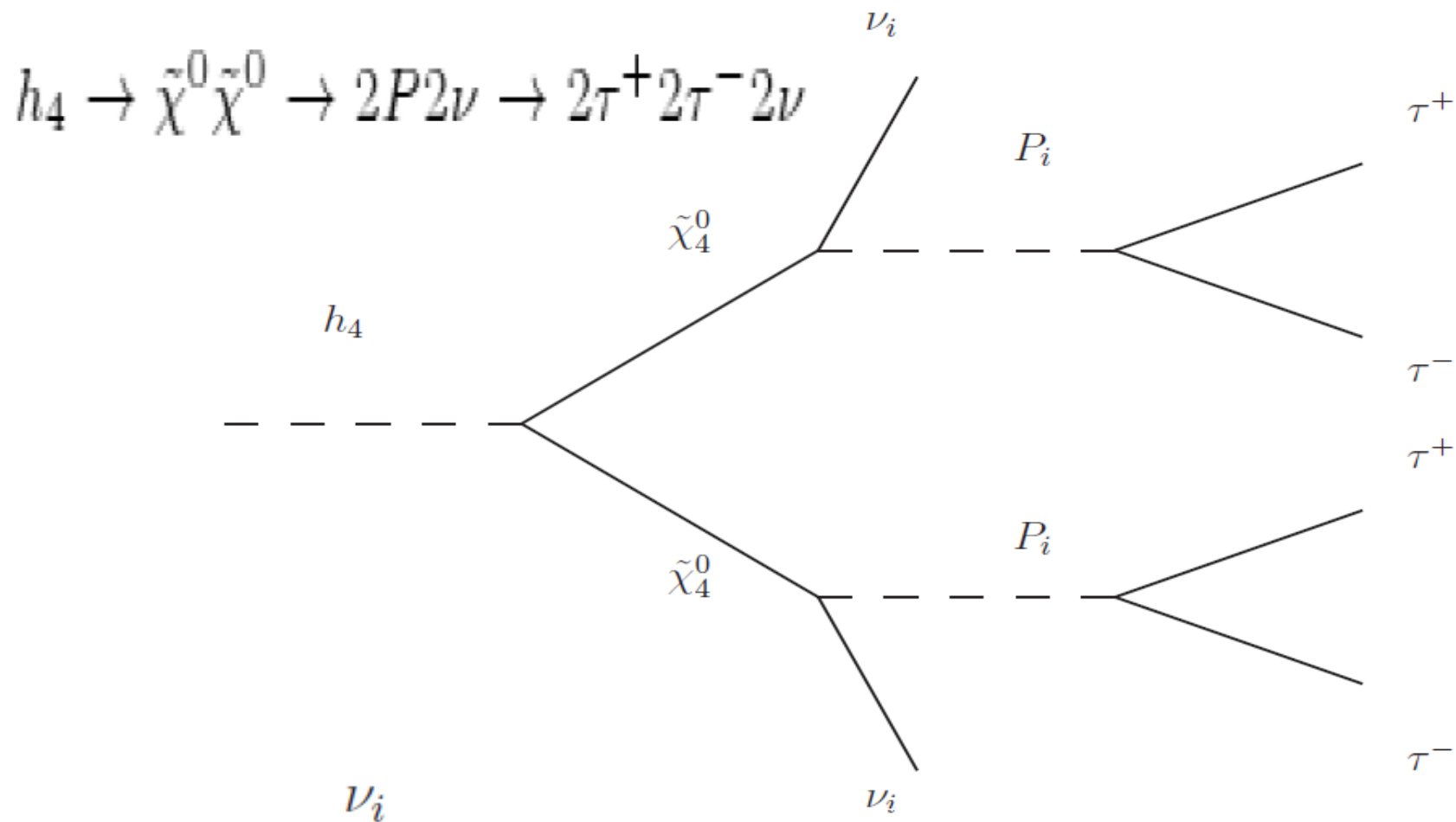
$$h_4 \rightarrow \tilde{\chi}^0 \tilde{\chi}^0 \rightarrow 2P2\nu \rightarrow 2\tau^+ 2\tau^- 2\nu$$

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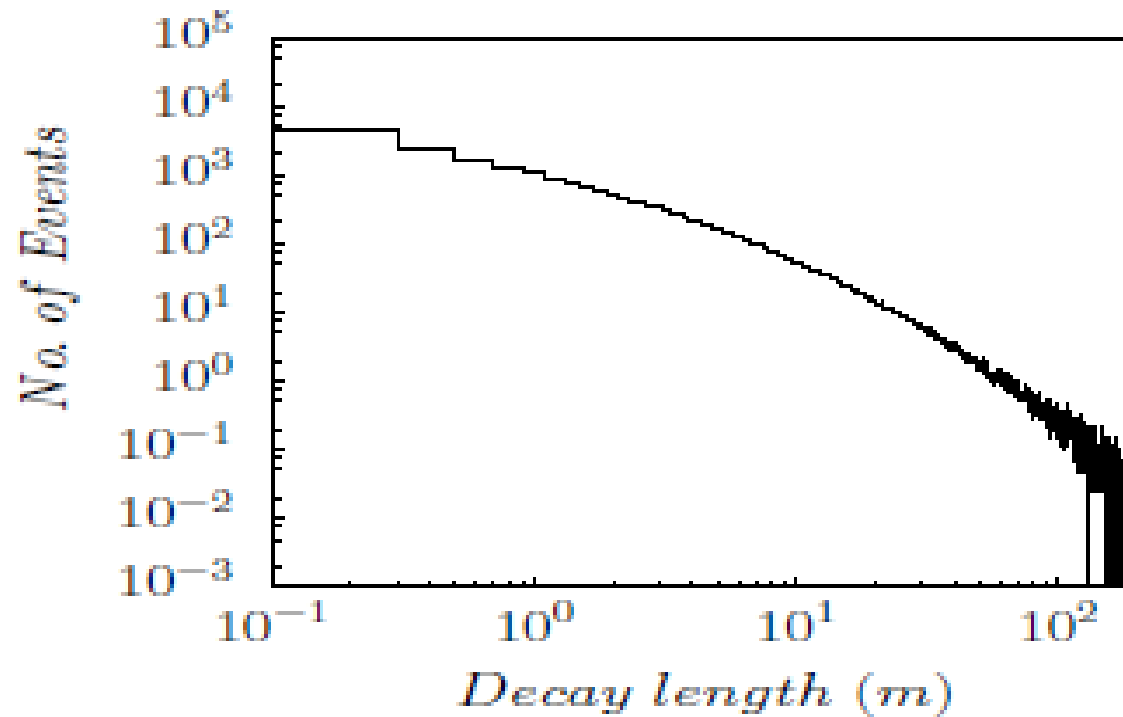
Displaced vertices signals (or missing energy if $\tilde{\chi}_4^0$ decays outside the detector)



$$Br(\tilde{\chi}_4^0 \rightarrow \sum_{i=1}^3 \tilde{\chi}_i^0 \tau^+ \tau^-) \approx 99\% \quad Br(h_4 \rightarrow \tilde{\chi}_4^0 \tilde{\chi}_4^0) \approx 6\%$$

$$m_{\tilde{\chi}_4^0} \approx 9.6 \text{ GeV} \quad m_{P_1} \approx 3.6 \text{ GeV}, m_{P_2} \approx 3.8 \text{ GeV} \quad m_{P_3} \approx 5.5 \text{ GeV}$$

Lightest Neutralino proper lifetime: $\tau_{\tilde{\chi}_4^0} \approx 10^{-9}$ s.



$\sqrt{s} = 8$ TeV with $\mathcal{L} = 20$ fb $^{-1}$

$$h_4 \rightarrow \tilde{\chi}^0 \tilde{\chi}^0 \rightarrow 2P2\nu \rightarrow 2\tau^+ 2\tau^- 2\nu$$

$$\sqrt{s} = 8 \text{ TeV with } \mathcal{L} = 20 \text{ fb}^{-1}$$

With τ decaying to e ,

μ ,

or hadronically

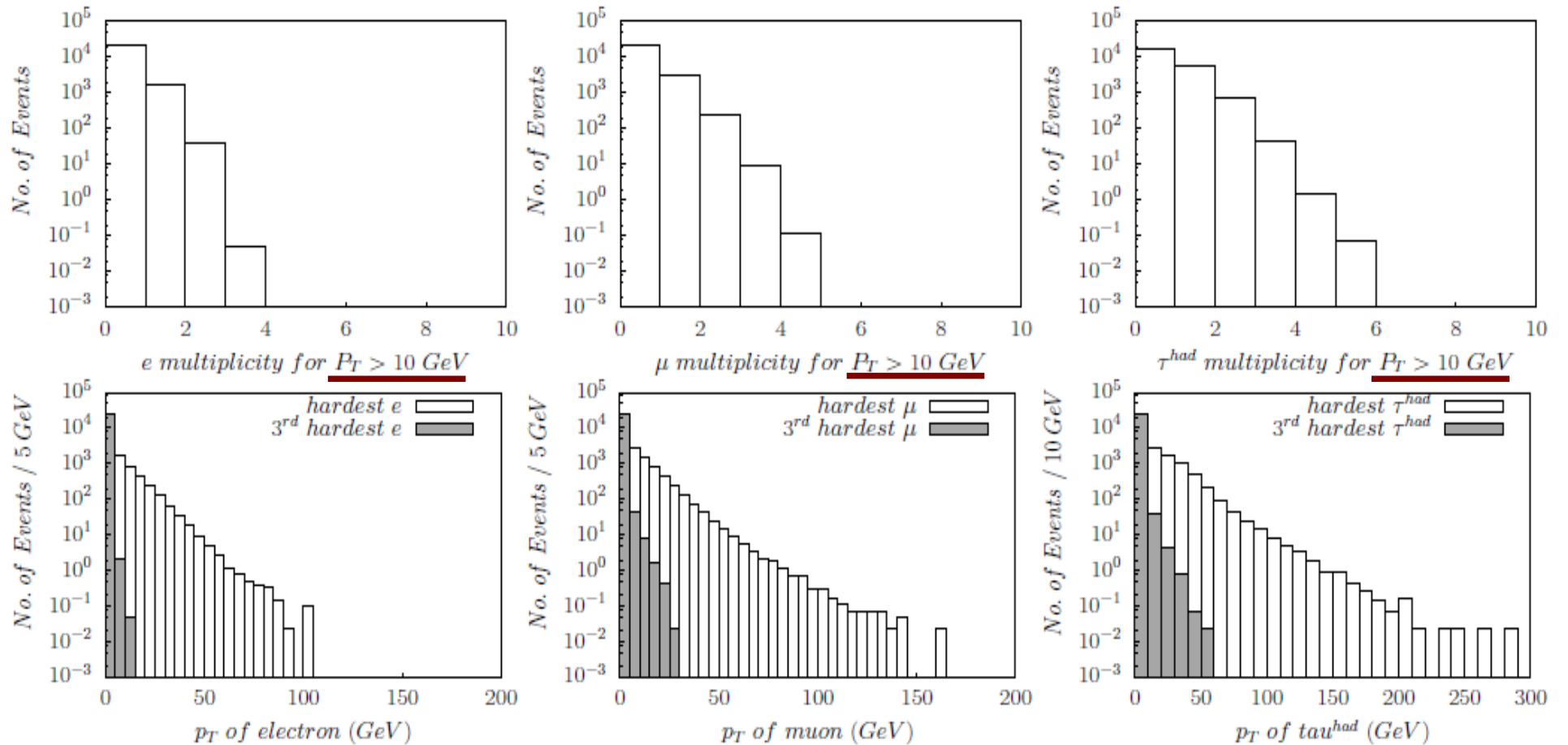
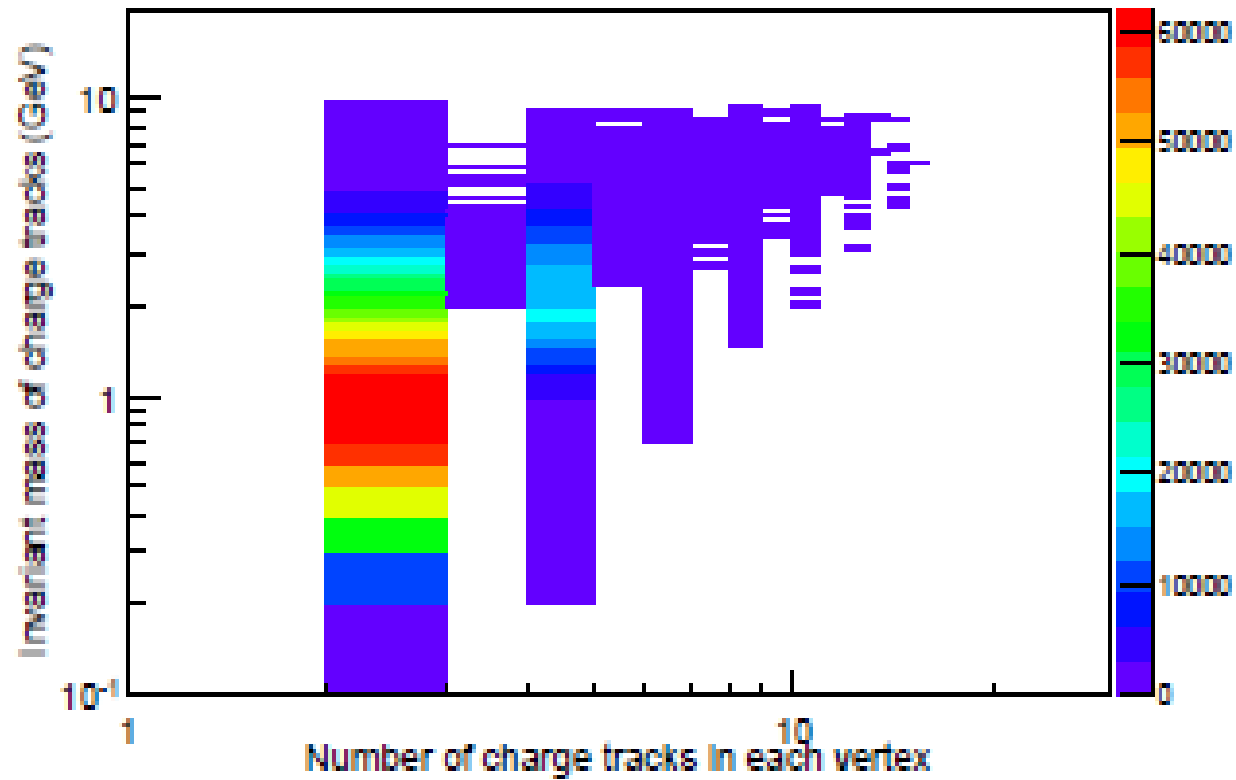
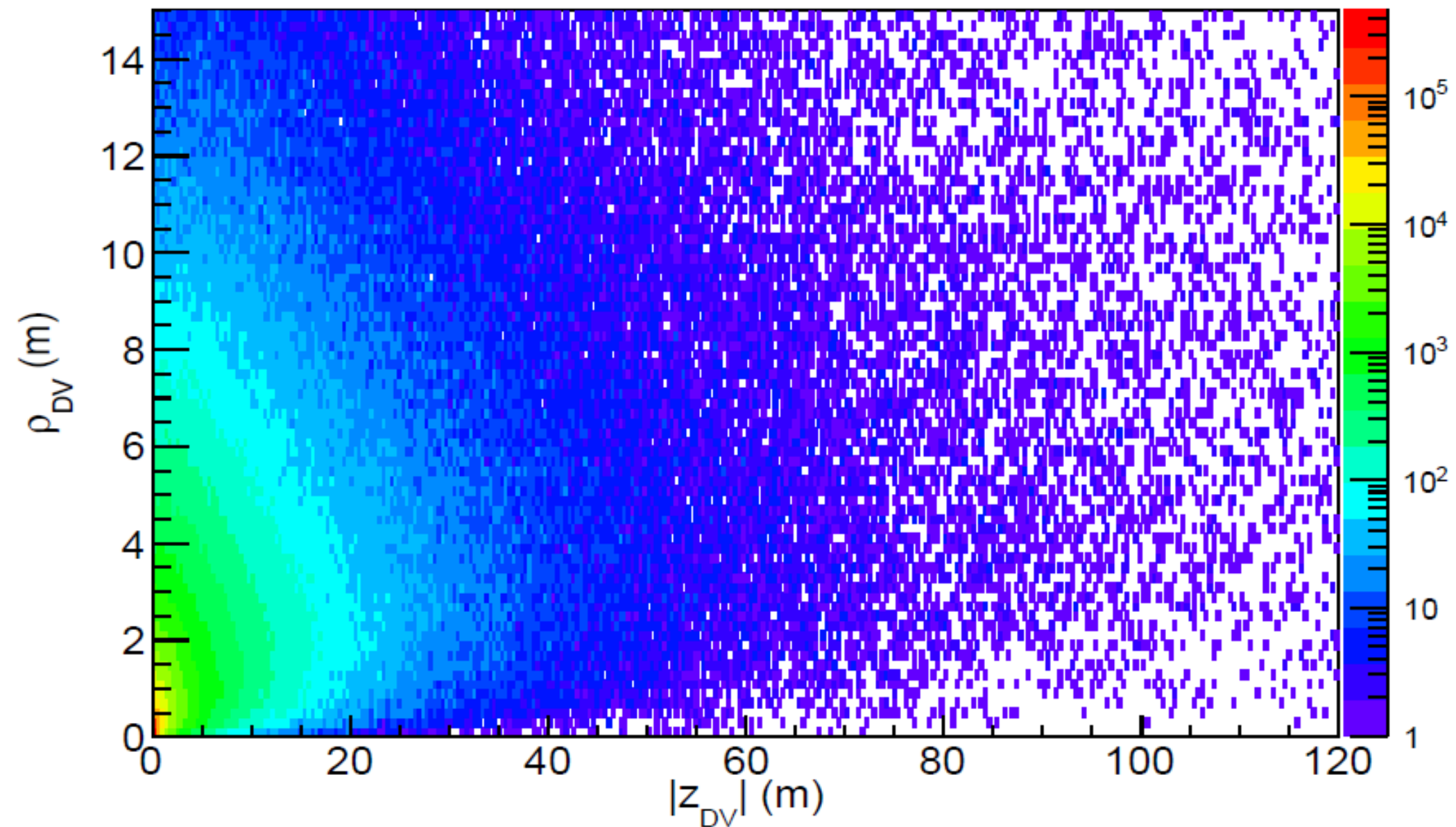


FIG. 1: Multiplicity (top row) for e (top left), μ (top middle) and hadronically decaying τ (top right) with $p_T > 10 \text{ GeV}$. p_T distributions (bottom row) for the leading (white) and the 3rd leading (light grey) e (bottom left), μ (bottom middle) and hadronically decaying τ (bottom right). These plots correspond to $\sqrt{s} = 8 \text{ TeV}$ with $\mathcal{L} = 20 \text{ fb}^{-1}$.

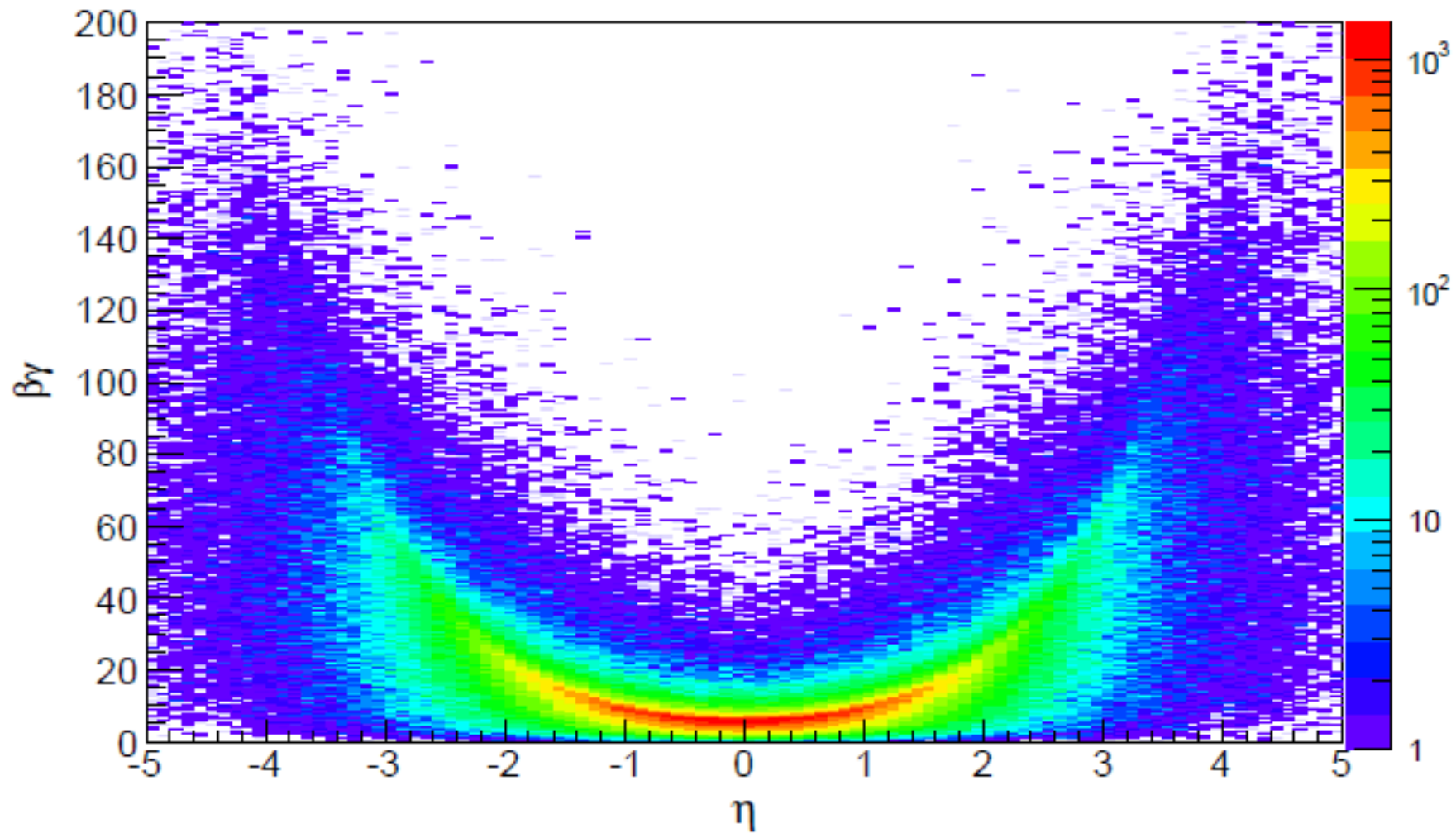
$$\sqrt{s} = 8 \text{ TeV with } \mathcal{L} = 20 \text{ fb}^{-1}$$



charged-track mass versus the number of charge particles



ρ_{DV} VERSUS $|z_{DV}|$



$\beta\gamma$ versus η (left)

Summary

The discovery of a Higgs candidate opens the door to discover new physics

Different possibilities of physics beyond the SM, for instance the $\mu\nu$ **SSM can be tested**