

Dinamica Cuantica

(* --- Calculo de las funciones de onda
en el oscilador armonico --- *)

phi[x_, n_Integer] :=

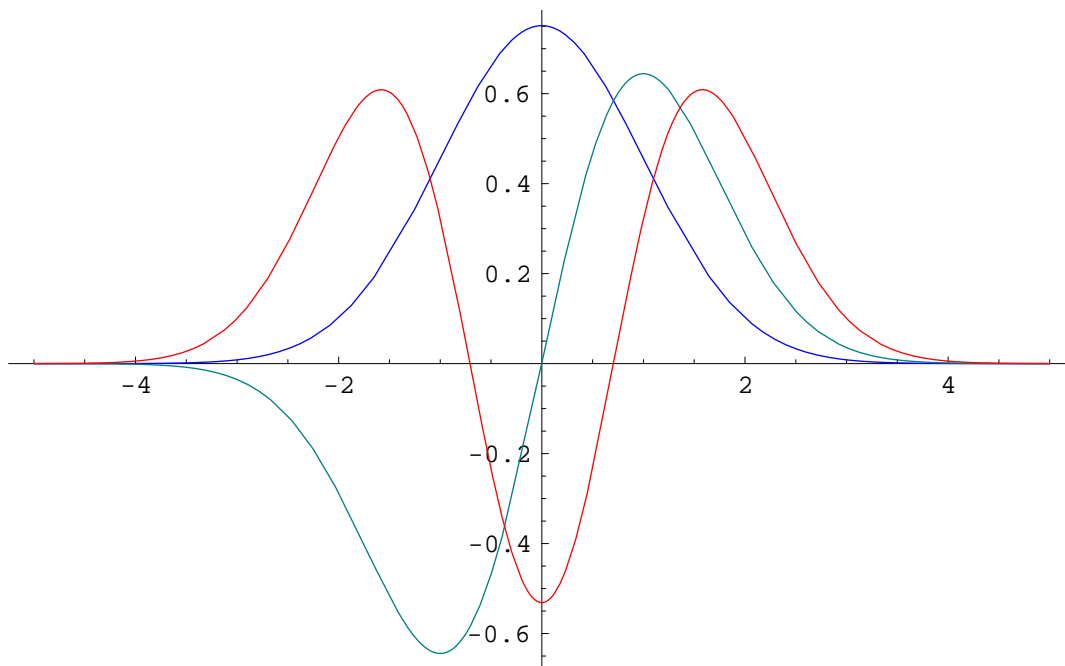
$$\sqrt{\frac{1}{\sqrt{\pi} * 2^n * n!}} * \text{Exp}\left[\frac{-x^2}{2}\right] * \text{HermiteH}[n, x]$$

(* ---- Energias ---- *)

$\omega = 1;$

Ener[n_Integer] := $\left(n + \frac{1}{2}\right) \omega;$

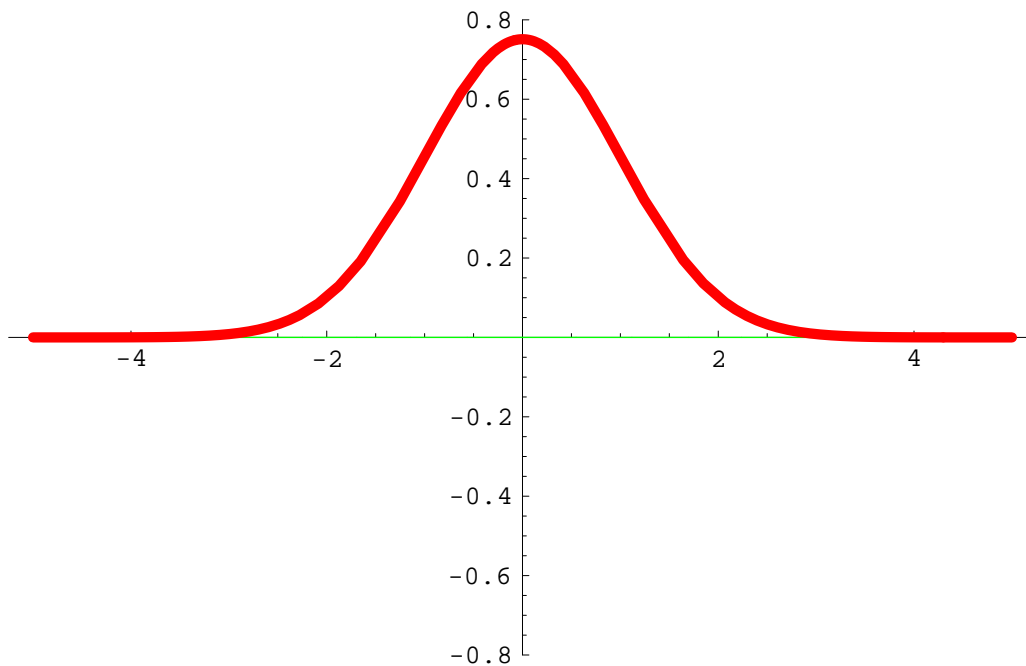
```
Plot[
  {phi[x, 0], phi[x, 1], phi[x, 2]}, {x, -5, 5},
  PlotStyle -> {{RGBColor[0, 0, 1]}, {RGBColor[0, .5, .5]},
    {RGBColor[1, 0, 0]}},
  ImageSize -> 500
];
```



```
(* ----- evolucion temporal
de onda estacionaria ----- *)
(* doble click en cualquier figura para ver la pelicula de la evolucion *)
```

```
 $\tau = 2 * \text{Pi} / (\text{Ener}[0]);$ 
```

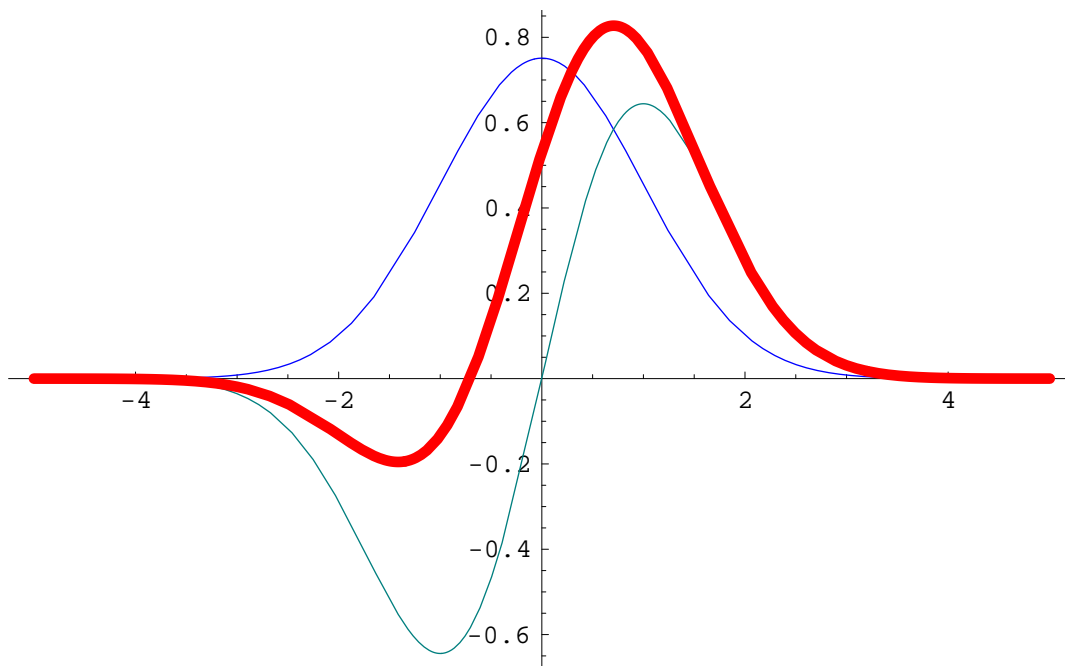
```
Table[Plot[
  { Re[ phi[x, 0] * Exp[- I * Ener[0] * t] ],
    Im[ phi[x, 0] * Exp[- I * Ener[0] * t] ],
    Abs[phi[x, 0] * Exp[- I * Ener[0] * t] ]
  },
  {x, -5, 5},
  PlotRange -> {-.8, .8},
  PlotStyle -> {
    {RGBColor[0, 0, 1]},
    {RGBColor[0, 1, 0]},
    {RGBColor[1, 0, 0], Thickness[0.01] }
  },
  ImageSize -> 500
],
{t, 0,  $\tau$ ,  $\tau/50$ }
];
```



```
(* ---- construccion de combinacion  
lineal de dos estados estacionarios ---- *)
```

```
c = {Sqrt[1./2.], Sqrt[1./2.]};
```

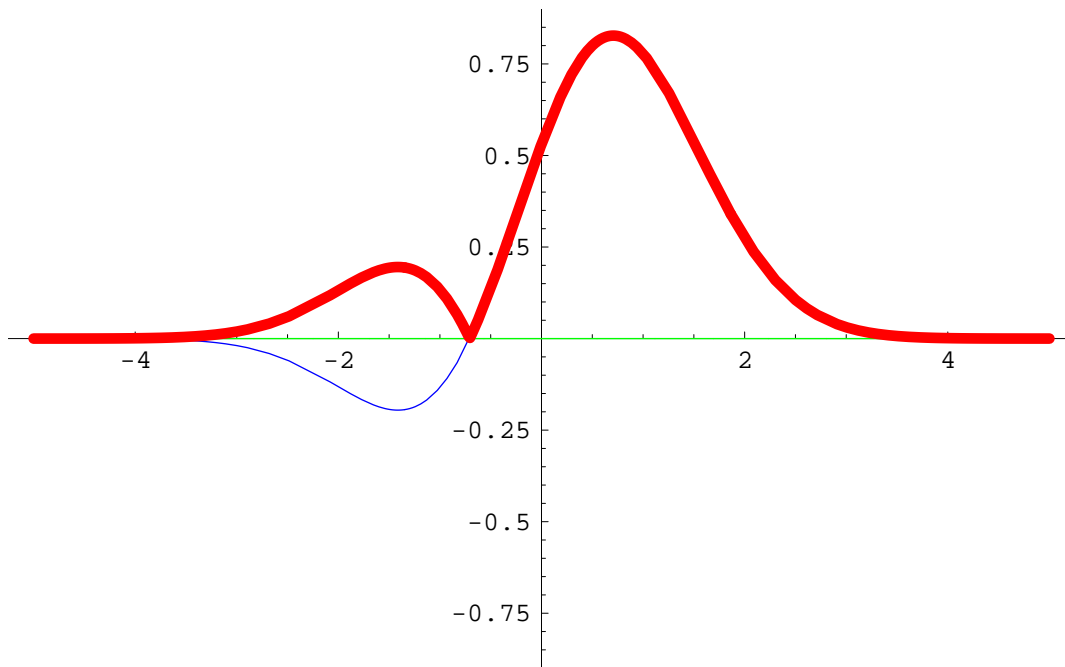
```
Plot[  
  {phi[x, 0], phi[x, 1],  
   c[[1]] phi[x, 0] + c[[2]] phi[x, 1]},  
  {x, -5, 5},  
  PlotStyle -> {  
    {RGBColor[0, 0, 1]    },  
    {RGBColor[0, 0.5, .5] },  
    {RGBColor[1, 0, 0], Thickness [ 0.01] }  
  },  
  ImageSize -> 500  
];
```



(* ---- evolucion temporal
de esta combinacion lineal ---- *)

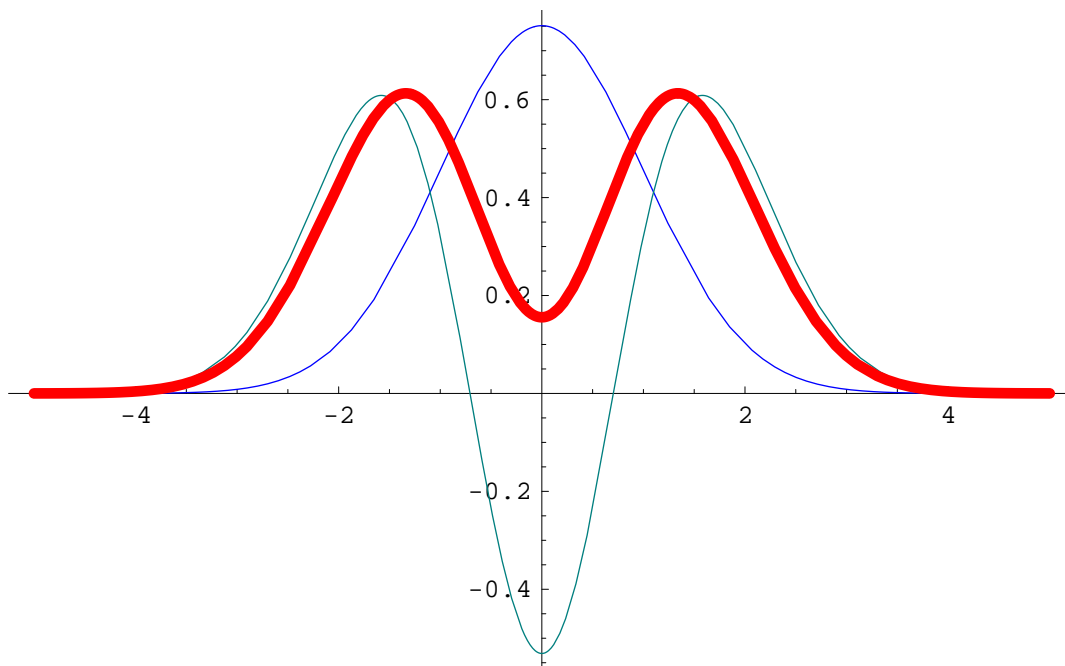
(* doble click en cualquier figura para ver la pelicula de la evolucion *)

```
Table[Plot[
  {Re[c[[1]] * phi[x, 0] * Exp[-I * Ener[0] * t] + c[[2]] * phi[x, 1] * Exp[-I * Ener[1] * t]],
    Im[c[[1]] * phi[x, 0] * Exp[-I * Ener[0] * t] + c[[2]] * phi[x, 1] * Exp[-I * Ener[1] * t]],
    Abs[c[[1]] * phi[x, 0] * Exp[-I * Ener[0] * t] +
      c[[2]] * phi[x, 1] * Exp[-I * Ener[1] * t]]},
  {x, -5, 5},
  PlotRange -> {-0.9, 0.9},
  PlotStyle -> {
    {RGBColor[0, 0, 1]},
    {RGBColor[0, 1, 0]},
    {RGBColor[1, 0, 0], Thickness[0.01]}
  },
  ImageSize -> 500
],
{t, 0, tau, tau/50}];
```



```
(* ---- combinacion lineal de  
funciones con misma paridad ---- *)
```

```
c = {Sqrt[1./2.], Sqrt[1./2.]};  
Plot[  
  {phi[x, 0], phi[x, 2],  
   c[[1]] phi[x, 0] + c[[2]] phi[x, 2]},  
  {x, -5, 5},  
  PlotStyle -> {  
    {RGBColor[0, 0, 1]      },  
    {RGBColor[0, 0.5, .5]  },  
    {RGBColor[1, 0, 0], Thickness [ 0.01] }  
  },  
  ImageSize -> 500  
];
```

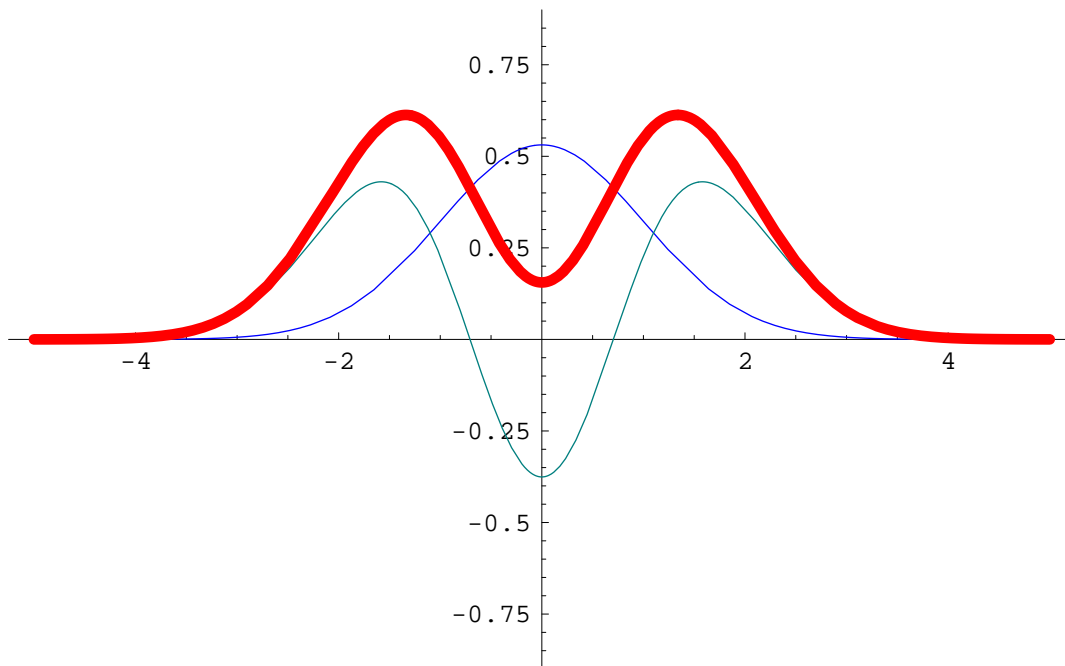


(* ---- evolucion temporal de la parte real ---- *)
 (* doble click en cualquier figura para ver la pelicula de la evolucion *)

```

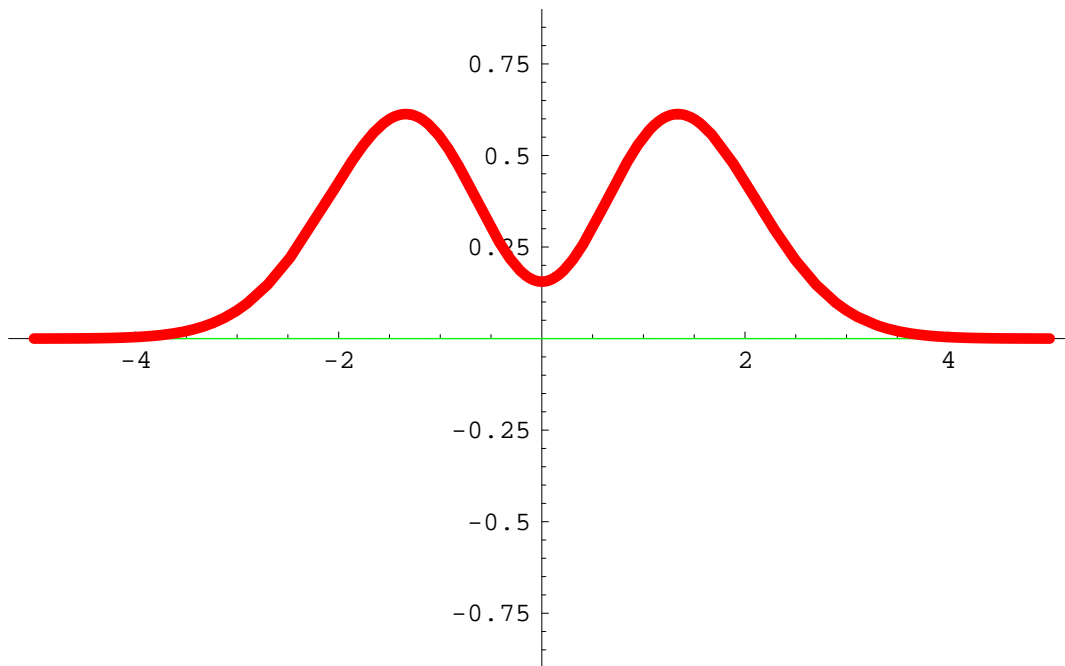
τ = 2 * Pi / (Ener[0]) ; movie1 = Table[Plot[{Re[c[[1]] * phi[x, 0] * Exp[- I * Ener[0] * t] ],
  Re[c[[2]] * phi[x, 2] * Exp[- I * Ener[2] * t] ],
  Re[c[[1]] * phi[x, 0] * Exp[- I * Ener[0] * t] +
  c[[2]] * phi[x, 2] * Exp[- I * Ener[2] * t]],
  {x, -5, 5},
  PlotRange → {- .9, .9},
  PlotStyle → {
    {RGBColor[0, 0, 1]},
    {RGBColor[0, 0.5, .5]},
    {RGBColor[1, 0, 0] , Thickness[0.01]}
  },
  ImageSize → 500
],
  {t, 0, τ, τ/50}
];

```



(* ---- funciones con la misma paridad ---- *)
 (* ---- Evolucion de la onda (Real,Imaginaria y Modulo) ---- *)
 (* doble click en cualquier figura para ver la pelicula de la evolucion *)

```
Table[Plot[
  {Re[c[[1]] * phi[x, 0] * Exp[-I * Ener[0] * t] + c[[2]] * phi[x, 2] * Exp[-I * Ener[2] * t]],
  Im[c[[1]] * phi[x, 0] * Exp[-I * Ener[0] * t] + c[[2]] * phi[x, 2] * Exp[-I * Ener[2] * t]],
  Abs[c[[1]] * phi[x, 0] * Exp[-I * Ener[0] * t] +
  c[[2]] * phi[x, 2] * Exp[-I * Ener[2] * t]]},
  {x, -5, 5},
  PlotRange -> {- .9, .9},
  PlotStyle -> {
    {RGBColor[0, 0, 1]},
    {RGBColor[0, 1, 0]},
    {RGBColor[1, 0, 0], Thickness[0.01]}
  },
  ImageSize -> 500
],
{t, 0, tau, tau / 50}];
```

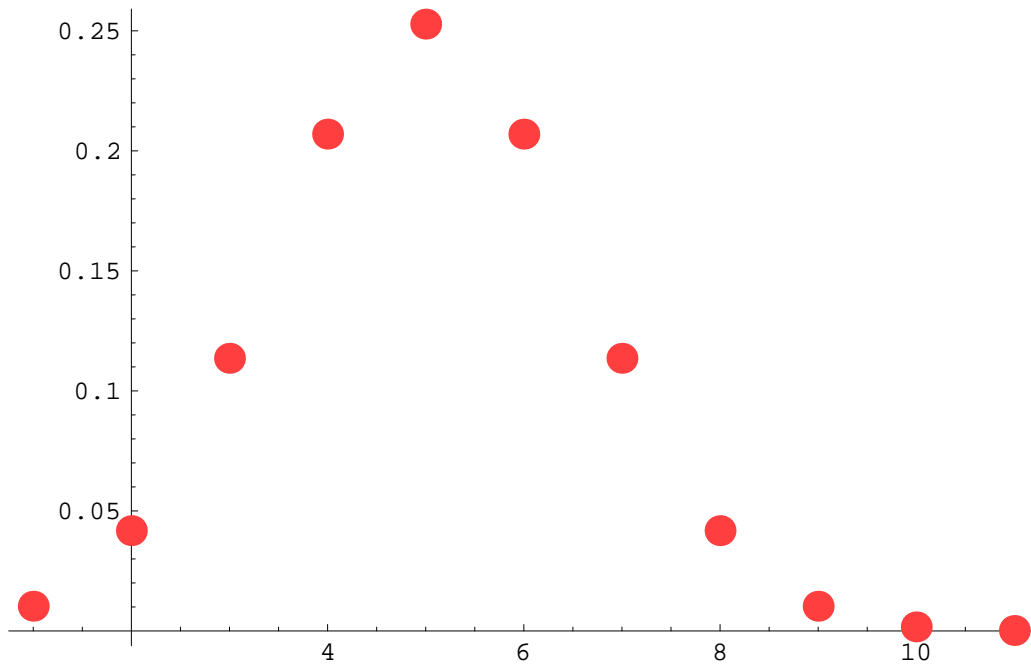


(* ---- Combinaciones generales
 de funciones estacionarias ---- *)

```
nmin = 1;
nmax = 11;
n0 = (nmax - nmin) / 2;
b := Table[ Exp[-(i - n0)^2 / n0], {i, nmin, nmax}]
Sumb = Sum[ (b[[n]]) , {n, nmin, nmax}];

b := Table[ Exp[-(i - n0)^2 / n0] / Sumb, {i, nmin, nmax}]
```

```
ListPlot[ b ,  
          PlotStyle -> {  
            RGBColor[1, 0.25, 0.25] , PointSize[0.03]  
          } ,  
          PlotRange -> All,  
          ImageSize -> 500  
        ] ;
```



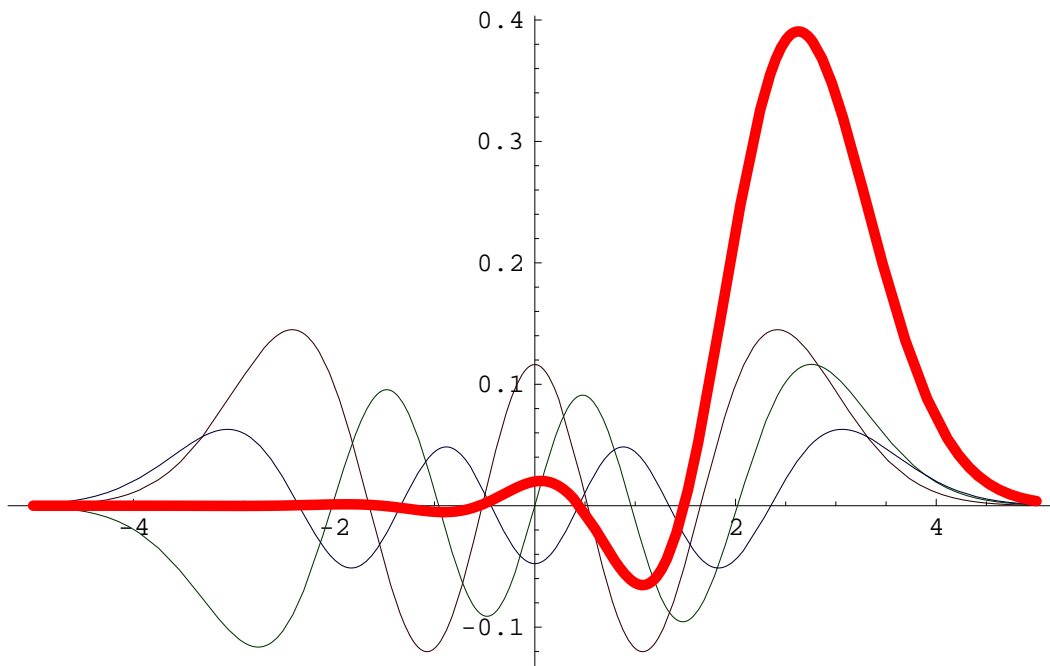
```
xi[x_] := Sum[  
  b[[n]] * phi[x, n - 1],  
  {n, nmin, nmax}  
] ;
```



```

Plot[ {b[[5]] * phi[x, 4], b[[6]] * phi[x, 5], b[[7]] * phi[x, 6], xi[x]}, {x, -5, 5},
  PlotRange -> All,
  PlotStyle -> {
    {RGBColor[0.2, 0, 0], Thickness[0.001] },
    {RGBColor[0.0, 0.2, 0], Thickness[0.001] },
    {RGBColor[0, 0, 0.2], Thickness[0.001] },
    {RGBColor[1, 0, 0], Thickness[0.01] },
  },
  ImageSize -> 500];

```



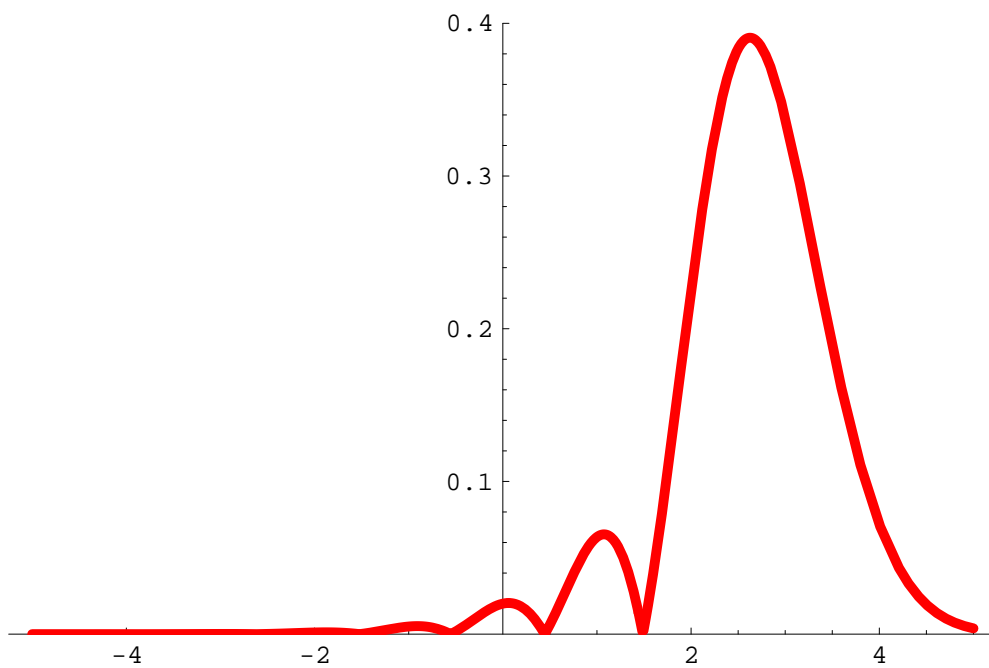
```

xi[x_, t_] := Sum[
  b[[n]] * phi[x, n - 1] * Exp[-I * Ener[n - 1] * t] ,
  {n, nmin, nmax}
];

```

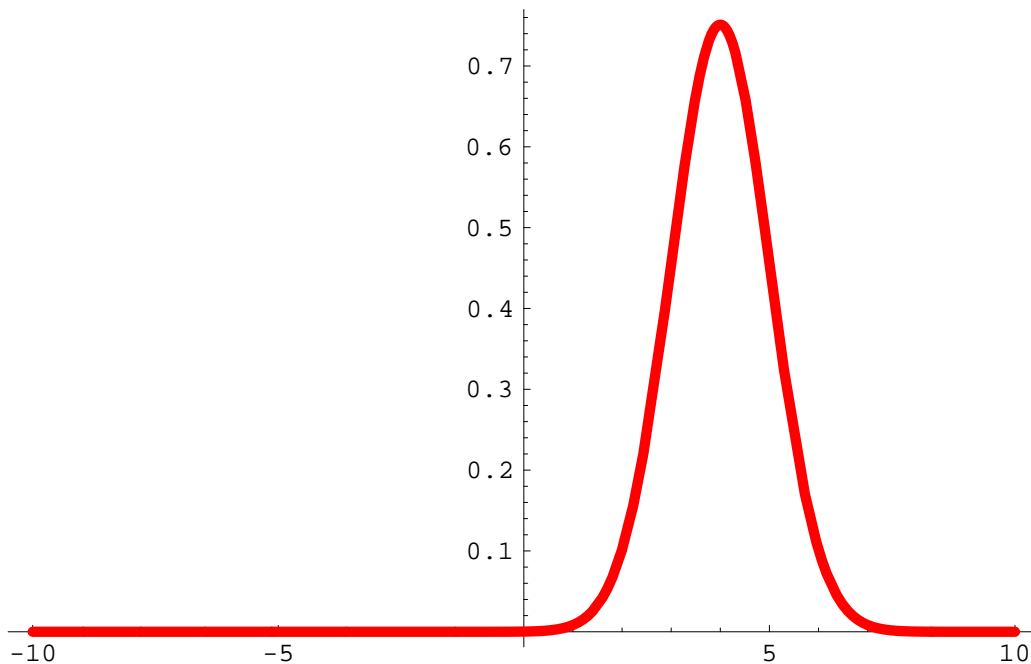
(* ---- Evolucion temporal
de esta combinacion ---- *)
(* doble click en cualquier figura para ver la pelicula de la evolucion *)

```
 $\tau = 1 * \text{Pi} / (\text{Ener}[0]);$   
Table[Plot[  
  Abs[  $\xi[x, t]$  ],  
  {x, -5, 5},  
  PlotRange -> {0., 0.4},  
  PlotStyle -> {  
    {RGBColor[1, 0, 0], Thickness[0.01]}  
  },  
  ImageSize -> 500  
],  
{t, 0,  $\tau$ ,  $\tau/25$ };
```



```
(* ---- Estado fundamental  
con traslacion espacial ---- *)
```

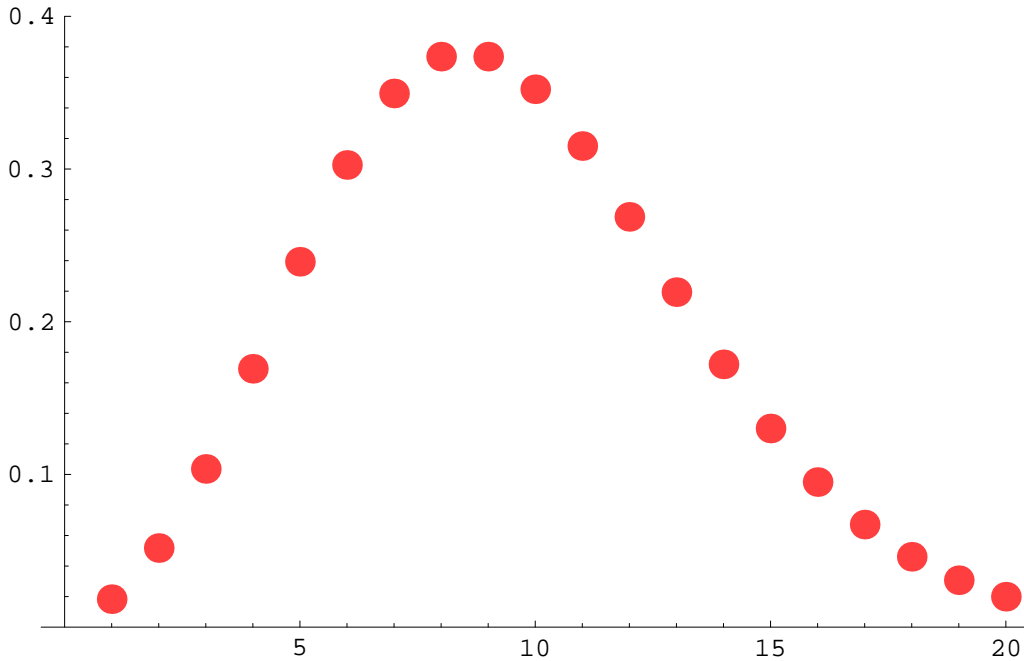
```
d = 4;  
Plot[phi[x - d, 0], {x, -10, 10},  
PlotRange -> All,  
PlotStyle -> {RGBColor[1, 0, 0], Thickness[0.01]},  
ImageSize -> 500];
```



```
(* ---- Coeficientes de la expansion  
en estados estacionarios ---- *)
```

```
f[n_Integer] := NIntegrate[phi[x - d, 0] * phi[x, n - 1], {x, -Infinity, Infinity}];  
nmin = 1;  
nmax = 20;  
b := Table[f[n], {n, nmin, nmax}];
```

```
ListPlot[ b ,
  PlotStyle -> {
    RGBColor[1, 0.25, 0.25] , PointSize[0.03]
  } ,
  PlotRange -> {0, 0.4},
  ImageSize -> 500
];
```



```
b[[n]]
```

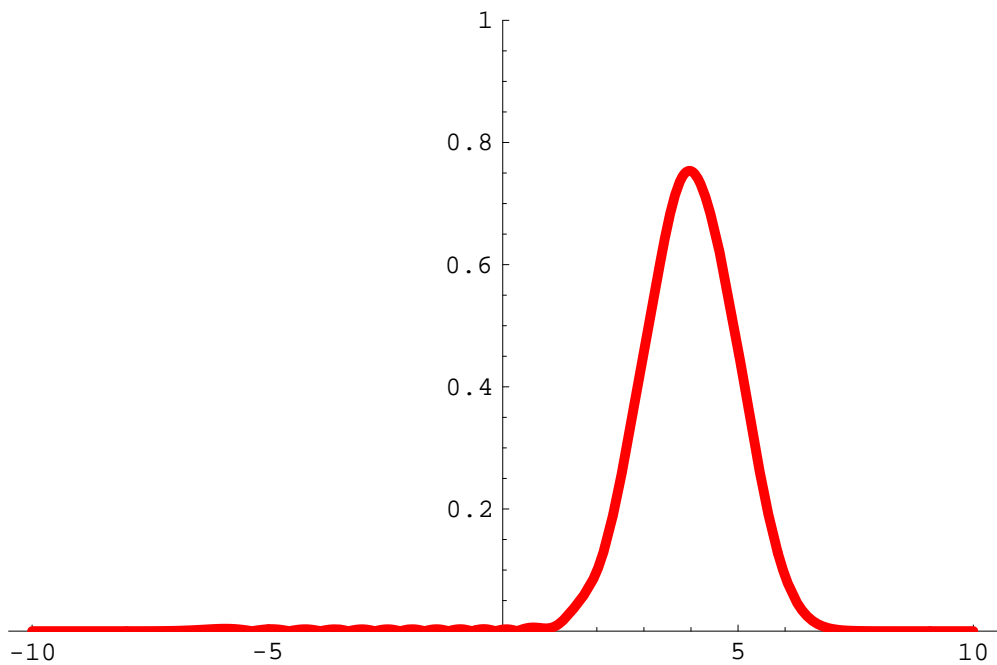
```
rrr = {0.018315638888889173`, 0.051804449838926805`,
  0.10360889968207333`, 0.16919262468414065`, 0.23927450447660478`,
  0.30266096808297815`, 0.34948278277392736`, 0.3736127972169554`,
  0.37361281027655086`, 0.35224553559712785`, 0.31505798504125754`,
  0.26868235234184806`, 0.2193782220055621`, 0.1720944359903972`,
  0.1300911657910072`, 0.09500515477277238`, 0.06717878889559205`,
  0.04608426913209869`, 0.030722846088117355`, 0.019935615014398337`}

{0.0183156, 0.0518044, 0.103609, 0.169193, 0.239275, 0.302661,
  0.349483, 0.373613, 0.373613, 0.352246, 0.315058, 0.268682, 0.219378,
  0.172094, 0.130091, 0.0950052, 0.0671788, 0.0460843, 0.0307228, 0.0199356}
```

```
 $\xi[x_, t_] := \text{Sum}[$ 
  rrr[[n]] * phi[x, n - 1] * Exp[-I * Ener[n - 1] * t] ,
  {n, nmin, nmax}
];
```

(* ---- Evolucion temporal
de estado coherente ---- *)
(* doble click en cualquier figura para ver la pelicula de la evolucion *)

```
 $\tau = 1 * \text{Pi} / (\text{Ener}[0]);$   
Table[Plot[  
  Abs[  $\xi[x, t]$  ],  
  {x, -10, 10},  
  PlotRange -> {0., 1},  
  PlotStyle -> {  
    {RGBColor[1, 0, 0], Thickness[0.01]}  
  },  
  ImageSize -> 500  
],  
{t, 0,  $\tau$ ,  $\tau/25$ };
```



```
(* HTMLSave["coherentes.html", "coherentes.nb"] *)
```