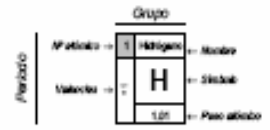


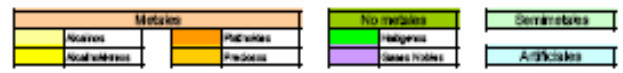
Tabla Periódica de los elementos

IA																												VIIA (01)	
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18											
1	H													He															
2	Li	Be											B	C	N	O	F	Ne											
3	Na	Mg											Al	Si	P	S	Cl	Ar											
4	K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr											
5	Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe											
6	Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn											
7	Fr	Ra	Ac	Unq	Unp	Unh	Uns	Unc	Uue																				



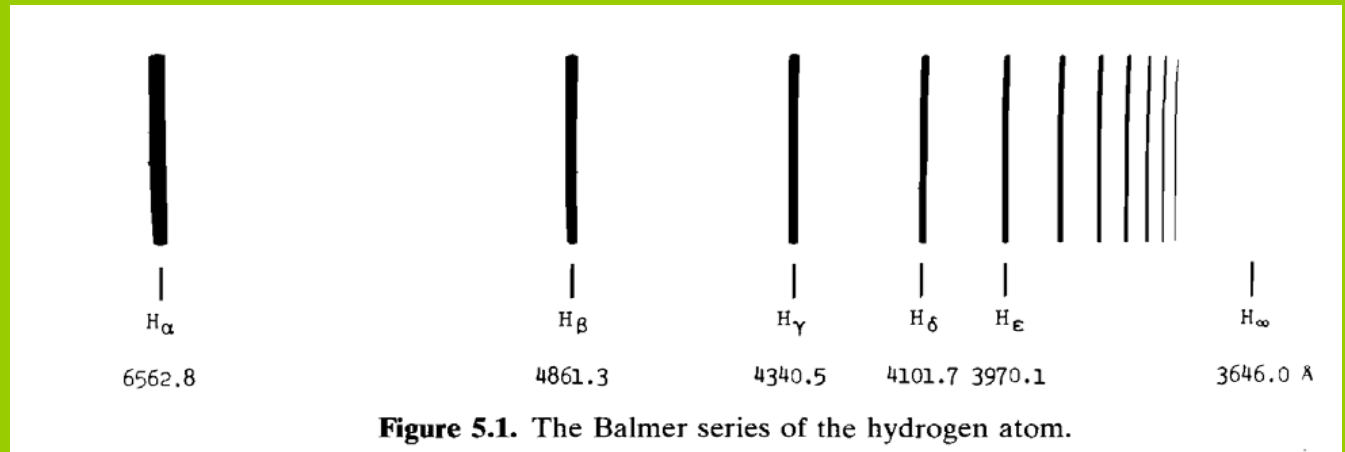
Tiempos Raras Ligeros (TRLA) Lantanidos		58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu
Tiempos Raras Pesadas (TRP)		90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr

* Número atómico del isótopo más ligero.
Peso atómico basado en ¹²C



ESPECTROS ATOMICOS

SERIE DE BALMER



$$\tilde{\nu} = 109,678 \left(\frac{1}{2^2} - \frac{1}{n^2} \right) \text{ cm}^{-1}, \quad n = 3, 4, \dots$$

$$= R_H \left(\frac{1}{2^2} - \frac{1}{n^2} \right),$$

$$\frac{-\hbar^2}{2mr^2} \frac{\partial}{\partial r} r^2 \frac{\partial \psi}{\partial r} + \frac{1}{2mr^2} \hat{L}^2 \psi - \frac{Ze^2 \psi}{4\pi\epsilon_0 r} = E\psi.$$

$$E_n = \frac{-\mu Z^2 (e^2 / 4\pi\epsilon_0)^2}{2n^2 \hbar^2} = \frac{-R}{n^2}, \quad n = 1, 2, 3, \dots,$$

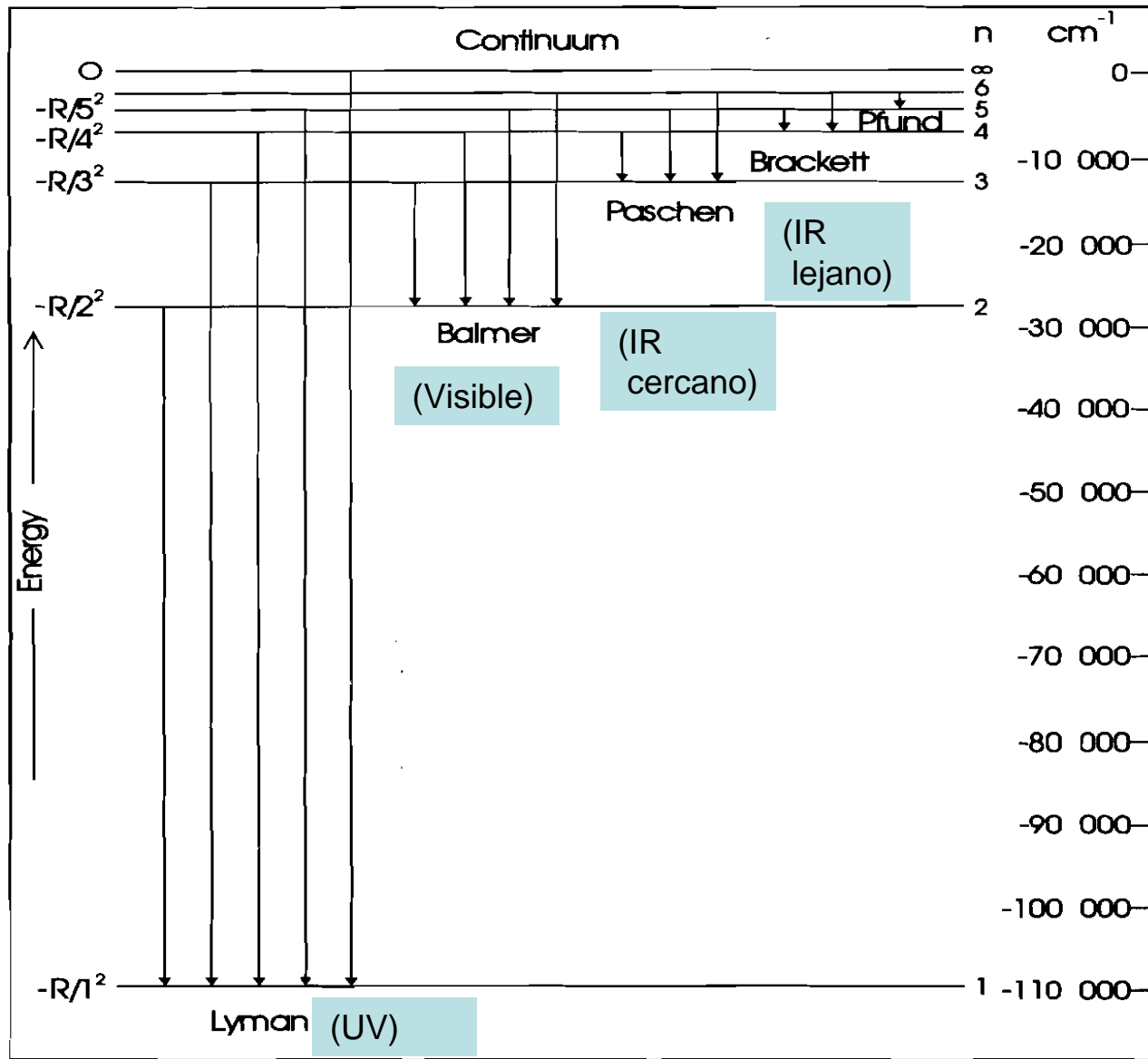


Figure 5.2. Energy levels of the hydrogen atom.

S=momento de spin electrónico

Matrices de Pauli

ATOMO DE HIDRÓGENO-espectro de un electrón

$$\frac{-\hbar^2}{2\mu} \nabla^2 \psi - \frac{Ze^2 \psi}{4\pi\epsilon_0 r} = E\psi.$$

$$\psi = R_{nl}(r) Y_{lm}(\theta, \phi),$$

$$E_n = \frac{-\mu Z^2 (e^2 / 4\pi\epsilon_0)^2}{2n^2 \hbar^2} = \frac{-R}{n^2}, \quad n = 1, 2, 3, \dots,$$

$$l = 0, 1, 2, 3, \dots \rightarrow s, p, d, f, \dots$$

$$R = R_H = 109,677,4212 \text{ cm}^{-1}$$

$$\frac{-\hbar^2}{2mr^2} \frac{\partial}{\partial r} r^2 \frac{\partial \psi}{\partial r} + \frac{1}{2mr^2} \hat{L}^2 \psi - \frac{Ze^2 \psi}{4\pi\epsilon_0 r} = E\psi.$$

$$n = 1, 2, 3, \dots, \infty,$$

$$l = 0, 1, \dots, n - 1,$$

$$m = 0, \pm 1, \dots, \pm l.$$

$$R_H = \frac{R_\infty}{1 + m_e/m_p},$$

Momento angular

$$[\hat{L}_x, \hat{L}_y] = i\hbar\hat{L}_z, \quad [\hat{L}_y, \hat{L}_z] = i\hbar\hat{L}_x, \quad [\hat{L}_z, \hat{L}_x] = i\hbar\hat{L}_y,$$

$$[\hat{L}^2, \hat{L}_x] = [\hat{L}^2, \hat{L}_y] = [\hat{L}^2, \hat{L}_z] = 0,$$

$$\hat{L}^2 Y_{LM}(\theta, \phi) = \hbar^2 L(L+1) Y_{LM}(\theta, \phi),$$

$$\hat{L}_z Y_{LM}(\theta, \phi) = M\hbar Y_{LM}(\theta, \phi).$$

$$L_+ = L_x + iL_y$$

Funciones de spin:

$$|\alpha\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \left| \frac{1}{2}; +\frac{1}{2} \right\rangle$$

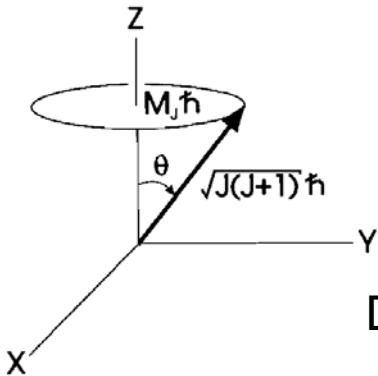
$$|\beta\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \left| \frac{1}{2}; -\frac{1}{2} \right\rangle$$

$$[\hat{H}, \hat{l}_z] = [\hat{H}, \hat{l}^2] = 0,$$

$$\hat{H}\psi_{nlm} = E_n\psi_{nlm},$$

$$\hat{l}^2\psi_{nlm} = l(l+1)\hbar^2\psi_{nlm},$$

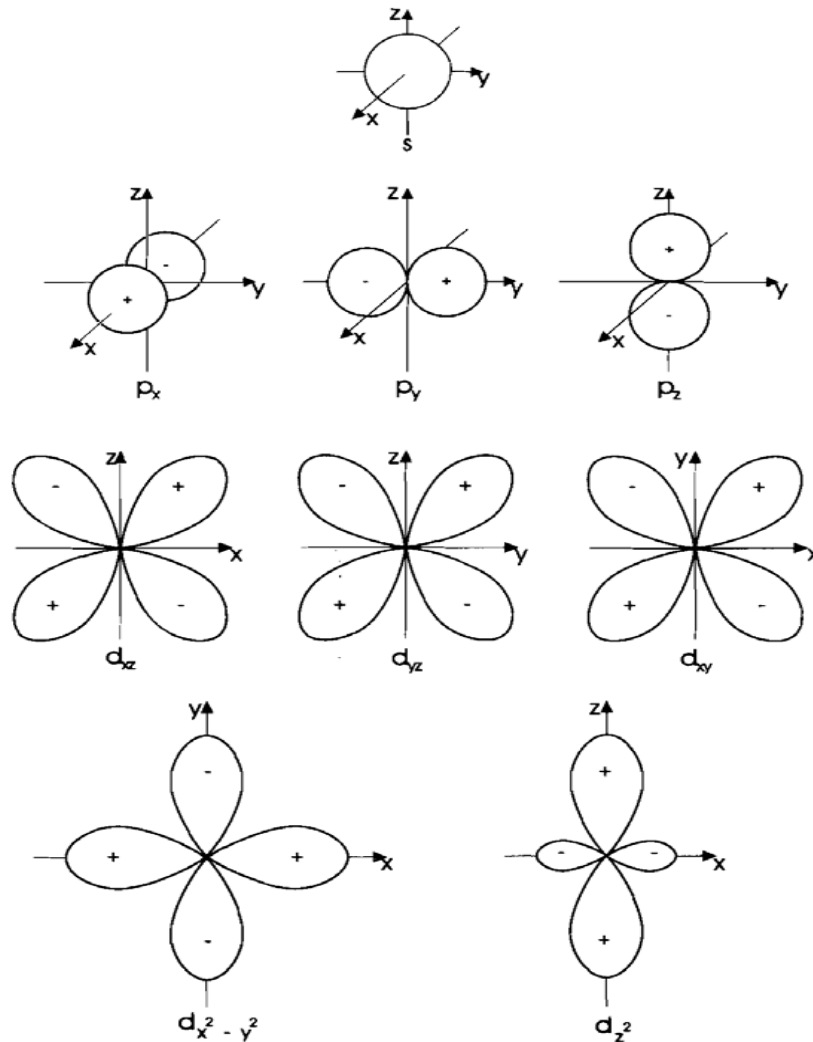
$$\hat{l}_z\psi_{nlm} = m\hbar\psi_{nlm}.$$



Degeneración $(2J+1)$

M_j : Diferentes orientaciones
Espaciales de \mathbf{J}

PARTE ANGULAR DE LOS ORBITALES 1s, 2p, 3d



$$\psi = R_{nl}(r)Y_{lm}(\theta, \phi),$$

Acoplamiento spin órbita

(estructura fina)

$$\boldsymbol{\mu}_s = -g_e \mu_B \mathbf{S}$$

$$E = -\boldsymbol{\mu} \cdot \mathbf{B}$$

Campo en el e^- proporcional a su
momento angular

$$\hat{H}_{so} = \xi(r) \hat{\mathbf{l}} \cdot \hat{\mathbf{s}}.$$

$$\xi(r) = \frac{1}{2\mu^2 c^2} \frac{1}{r} \frac{\partial V}{\partial r} = \frac{1}{2\mu^2 c^2} \left(\frac{Ze^2}{4\pi\epsilon_0 r^3} \right)$$

$$V = -\frac{Ze^2}{4\pi\epsilon_0 r}$$

Atracción COULOMBIANA
entre electrón y núcleos

$$[\hat{H}^{(0)} + \xi(r)\hat{\mathbf{l}} \cdot \hat{\mathbf{s}}]\psi = E\psi,$$

(derivación adecuada: EQR
(electrodinámica cuántica relativista))

\mathbf{l} y \mathbf{s} no conmutan con \mathbf{H}

$$\mathbf{j} = \mathbf{l} + \mathbf{s}$$

\mathbf{j} conmuta con \mathbf{H}

(cte de movimiento)

j^2 y j_z **SI** conmutan con \mathbf{H}

Ejemplo:
electrones p

$$|l = 1, m_l = 1\rangle |s = \frac{1}{2}, m_s = \pm \frac{1}{2}\rangle,$$
$$|l = 1, m_l = 0\rangle |s = \frac{1}{2}, m_s = \pm \frac{1}{2}\rangle,$$

(Representación desacoplada:
Producto de funciones angular
y spin de un electrón)

$$|l = 1, m_l = -1\rangle |s = \frac{1}{2}, m_s = \pm \frac{1}{2}\rangle.$$

Representación en estados acoplados y desacoplados

$$\hat{H} = \hat{H}^{(0)} + \xi(r)\hat{\mathbf{l}} \cdot \hat{\mathbf{s}} = (\hat{H}^{(0)} + \xi(r)\hat{l}_z\hat{s}_z) + \frac{\xi(r)(\hat{l}_+\hat{s}_- + \hat{l}_-\hat{s}_+)}{2}$$

$$\begin{aligned} \langle l = 1, m_l | \langle s = \frac{1}{2}, m_s | \hat{H} | s = \frac{1}{2}, m_s \rangle | l = 1, m_l \rangle \\ = E_{2p}^{(0)} + \zeta_{2p} m_l m_s \end{aligned}$$

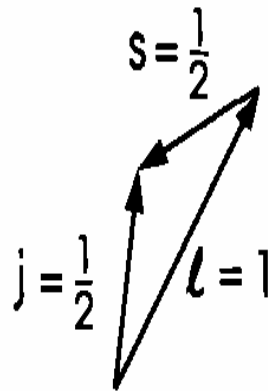
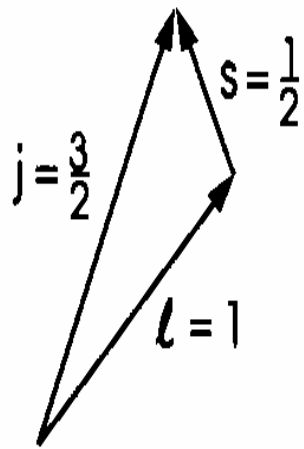
$$E_{2p}^{(0)} = -R_H/4$$

$$\zeta_{2p} = \hbar^2 \int R_{2p}^*(r) \xi(r) R_{2p}(r) r^2 dr.$$

$$\xi \hat{\mathbf{l}} \cdot \hat{\mathbf{s}} = \frac{\xi(\hat{j}^2 - \hat{l}^2 - \hat{s}^2)}{2}.$$

$$\hat{j}^2 = (\hat{\mathbf{l}} + \hat{\mathbf{s}}) \cdot (\hat{\mathbf{l}} + \hat{\mathbf{s}}) = \hat{\mathbf{l}}^2 + \hat{\mathbf{s}}^2 + 2\hat{\mathbf{l}} \cdot \hat{\mathbf{s}}$$

J^2 conmuta con H



Los estados acoplados están relacionados con los no acoplados por

Aparecen los coeficientes de Glebsh Gordan

$$|j_1, j_2 J, M_J\rangle = \sum_{m_1=-j_1}^{j_1} \sum_{m_2=-j_2}^{j_2} \langle j_1, j_2; m_1, m_2 | JM_J\rangle |j_1 m_1\rangle |j_2 m_2\rangle,$$

$$|2p, j = \frac{3}{2}, m_j = \frac{3}{2}\rangle,$$

$$|2p, j = \frac{3}{2}, m_j = \frac{1}{2}\rangle,$$

$$|2p, j = \frac{3}{2}, m_j = -\frac{1}{2}\rangle,$$

$$|2p, j = \frac{3}{2}, m_j = -\frac{3}{2}\rangle,$$

$$|2p, j = \frac{1}{2}, m_j = \frac{1}{2}\rangle,$$

$$|2p, j = \frac{1}{2}, m_j = -\frac{1}{2}\rangle.$$

SISTEMA DE MUCHOS ELECTRONES

$$\left(\frac{-\hbar^2}{2m_e} \sum_{i=1}^N \nabla_i^2 - \sum_{i=1}^N \frac{Ze^2}{4\pi\epsilon_0 r_i} + \sum_{i,j>i}^N \frac{e^2}{4\pi\epsilon_0 r_{ij}} \right) \psi = E\psi.$$

$$\hat{\mathbf{L}} = \hat{\mathbf{l}}_1 + \hat{\mathbf{l}}_2 + \cdots + \hat{\mathbf{l}}_N = \sum_{i=1}^N \hat{\mathbf{l}}_i.$$

$$\hat{\mathbf{S}} = \sum_{i=1}^N \hat{\mathbf{s}}_i$$

$$\hat{\mathbf{J}} = \hat{\mathbf{L}} + \hat{\mathbf{S}}.$$

$$\hat{L}_z = \hat{l}_{z1} + \hat{l}_{z2} + \cdots + \hat{l}_{zN},$$

$$\hat{S}_z = \hat{s}_{z1} + \hat{s}_{z2} + \cdots + \hat{s}_{zN},$$

$$\hat{L}^2 = \hat{L}_x^2 + \hat{L}_y^2 + \hat{L}_z^2,$$

$$\hat{S}^2 = \hat{S}_x^2 + \hat{S}_y^2 + \hat{S}_z^2.$$

$$\hat{L}^2 \psi \approx L(L + 1)\hbar^2 \psi$$

$$[\hat{l}_{zi}, \hat{H}] \neq 0,$$

$$\hat{l}_{zi} \psi \neq m_{li} \hbar \psi,$$

$$\hat{L}_z \psi = M_L \hbar \psi,$$

$$M_L = m_{l1} + m_{l2} + \cdots + m_{lN}.$$

$$[\hat{L}_z, \hat{H}] = 0,$$

$$[\hat{L}_x, \hat{H}] = 0 \quad \text{and} \quad [\hat{L}_y, \hat{H}] = 0.$$

$$[\hat{L}_z^2, \hat{H}] = 0, \quad [\hat{L}_x^2, \hat{H}] = 0, \quad \text{and} \quad [\hat{L}_y^2, \hat{H}] = 0,$$

$$[\hat{L}^2, \hat{H}] = 0$$

Table 5.4. One-electron and Multi-electron Atoms

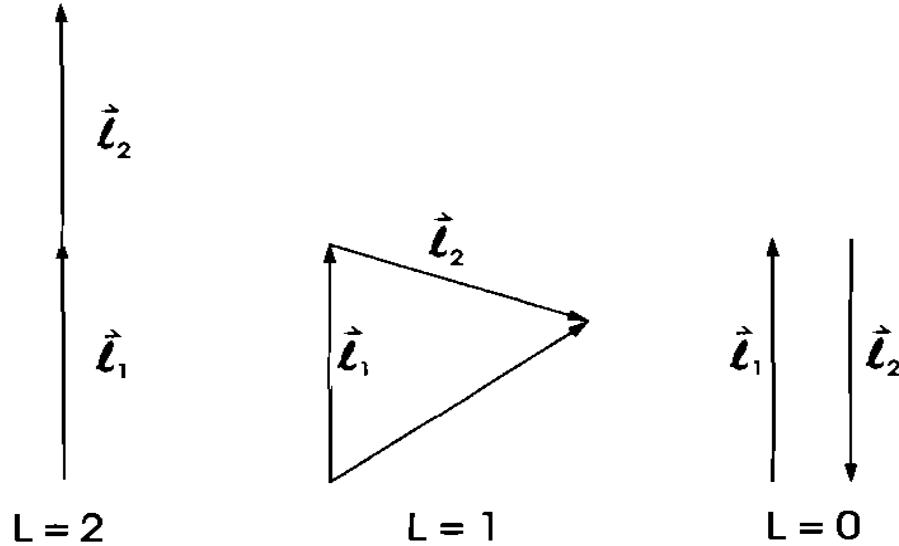
Multi-electron Atoms						One-electron Atoms					
$\hat{L}^2\psi = L(L + 1)\hbar^2\psi$						$\hat{l}^2\psi = l(l + 1)\hbar^2\psi$					
$\hat{L}_z\psi = M_L\hbar\psi$						$\hat{l}_z\psi = m_l\hbar\psi$					
$\hat{S}^2\psi = S(S + 1)\hbar^2\psi$						$\hat{s}^2\psi = s(s + 1)\hbar^2\psi$					
$\hat{S}_z\psi = M_S\hbar\psi$						$\hat{s}_z\psi = m_s\hbar\psi$					
$L = 0,$	$1,$	$2,$	$3,$	$4,$	5	$l = 0,$	$1,$	$2,$	$3,$	$4,$	5
S	P	D	F	G	H	s	p	d	f	g	h

$$2S+1 L,$$

Degeneración
→

$$g = (2L + 1)(2S + 1).$$

Ejemplo $l_1=1, l_2=1$



Configuración $2p^2$
átomo de Carbono

$$\chi_1 = p_1 \alpha, \chi_2 = p_0 \alpha, \chi_3 = p_{-1} \alpha,$$

$$\chi_4 = p_1 \beta, \chi_5 = p_0 \beta, \chi_6 = p_{-1} \beta$$

2 electrones y
6 spin orbitales

15
determinantes

	$M_S = 1$	0	-1
$M_L = 2$	—	$ 1, \bar{1} $	—
$M_L = 1$	$ 1, 0 $	$ 1, \bar{0} 1, 0 $	$ \bar{1}, \bar{0} $
$M_L = 0$	$ 1, -1 $	$ 1, -\bar{1} 1, -1 0, \bar{0} $	$ \bar{1}, -\bar{1} $
$M_L = -1$	$ 0, -1 $	$ -1, \bar{0} -\bar{1}, 0 $	$ \bar{0}, -\bar{1} $
$M_L = -2$	—	$ -1, -\bar{1} $	—

microestado

15 configuraciones: no todas spin adaptadas

Notación

$|1, \bar{0}|$

significa.

$$m_{l1} = 1, m_{s1} = \frac{1}{2}, m_{l2} = 0, m_{s2} = -\frac{1}{2}$$

Acoplamiento Spin órbita

$$\hat{H}_{so} = \zeta \hat{\mathbf{L}} \cdot \hat{\mathbf{S}}.$$

Valores permitidos

$$J=L+S, L+S-1, \dots, |L-S|$$

$$\hat{J}^2 = (\mathbf{L} + \mathbf{S}) \cdot (\mathbf{L} + \mathbf{S}) = \hat{L}^2 + \hat{S}^2 + 2\mathbf{L} \cdot \mathbf{S}.$$

$$\mathbf{L} \cdot \mathbf{S} = \frac{\hat{J}^2 - \hat{L}^2 - \hat{S}^2}{2}$$

Las **componentes** de **L** y **S** no conmutan con H

$$\mathbf{J} = \mathbf{L} + \mathbf{S}$$

J, **L**² y **S**² conmutan con H

$$\begin{aligned} \langle H_{so} \rangle &= \zeta \langle \mathbf{L} \cdot \mathbf{S} \rangle = \zeta \langle nJM_JLS | \mathbf{L} \cdot \mathbf{S} | nJM_JLS \rangle \\ &= \frac{\zeta [J(J+1) - L(L+1) - S(S+1)]}{2}. \end{aligned}$$

$$\hat{H} = \hat{H}_0 + \hat{H}_{ee}$$

$$\hat{H} = \hat{H}_0 + \hat{H}_{ee} + \zeta \mathbf{L} \cdot \mathbf{S}$$

$$\hat{H} = \hat{H}_0 + \hat{H}_{ee} + \sum \xi(r_i) \mathbf{l}_i \cdot \mathbf{s}_i$$

$$\hat{H}\psi = E\psi$$

$$\hat{L}^2\psi = L(L+1)\hbar^2\psi$$

$$\hat{L}_z\psi = M_L\hbar\psi$$

$$\hat{S}^2\psi = S(S+1)\hbar^2\psi$$

$$\hat{S}_z\psi = M_S\hbar\psi$$

$$\hat{H}\psi = E\psi$$

$$\hat{L}^2\psi = L(L+1)\hbar^2\psi$$

$$\hat{S}^2\psi = S(S+1)\hbar^2\psi$$

$$\hat{J}^2\psi = J(J+1)\hbar^2\psi$$

$$\hat{J}_z\psi = M_J\hbar\psi$$

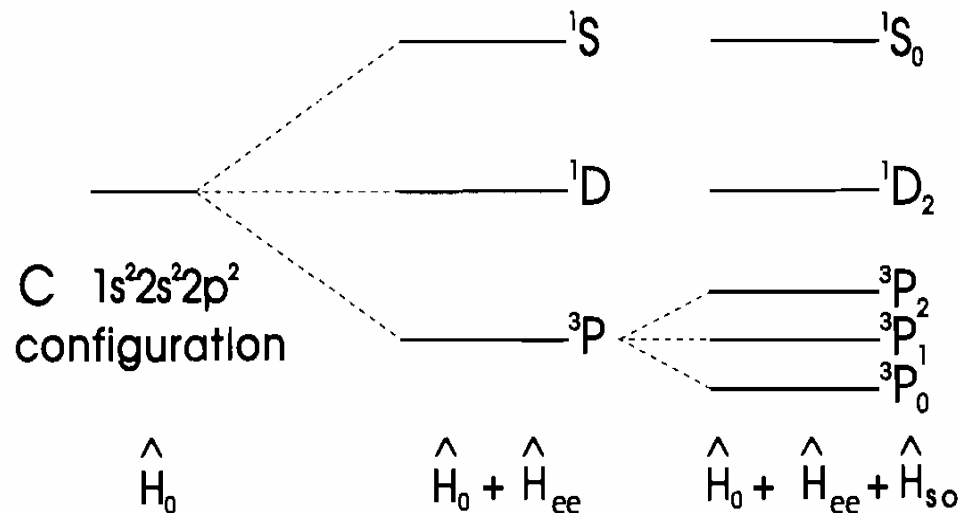
$$\hat{H}\psi = E\psi$$

$$\hat{L}^2\psi \approx L(L+1)\hbar^2\psi$$

$$\hat{S}^2\psi \approx S(S+1)\hbar^2\psi$$

$$\hat{J}^2\psi = J(J+1)\hbar^2\psi$$

$$\hat{J}_z\psi = M_J\hbar\psi$$



Reglas de selección

Regla de Hund

- Al llenar orbitales de igual energía, los electrones prefieren acomodarse con spin paralelo

Ejemplo: **3 electrones en el orbital 2p;**

$px^1 py^1 pz^1$ (vs) $px^2 py^1 pz^0$

$(px^2 py^1 pz^0 = px^0 py^1 pz^2 = px^1 py^0 pz^2 = px^2 py^0$

$pz^1 = \dots)$

1era. Regla: mayor proyección de spin.

2da. Regla mayor Momento angular.

3era. Regla Acoplamiento spin órbita.

Cuando varios electrones están descritos por orbitales degenerados, la mayor estabilidad energética es aquella en donde los espines electrónicos están desapareados (correlación de espines):

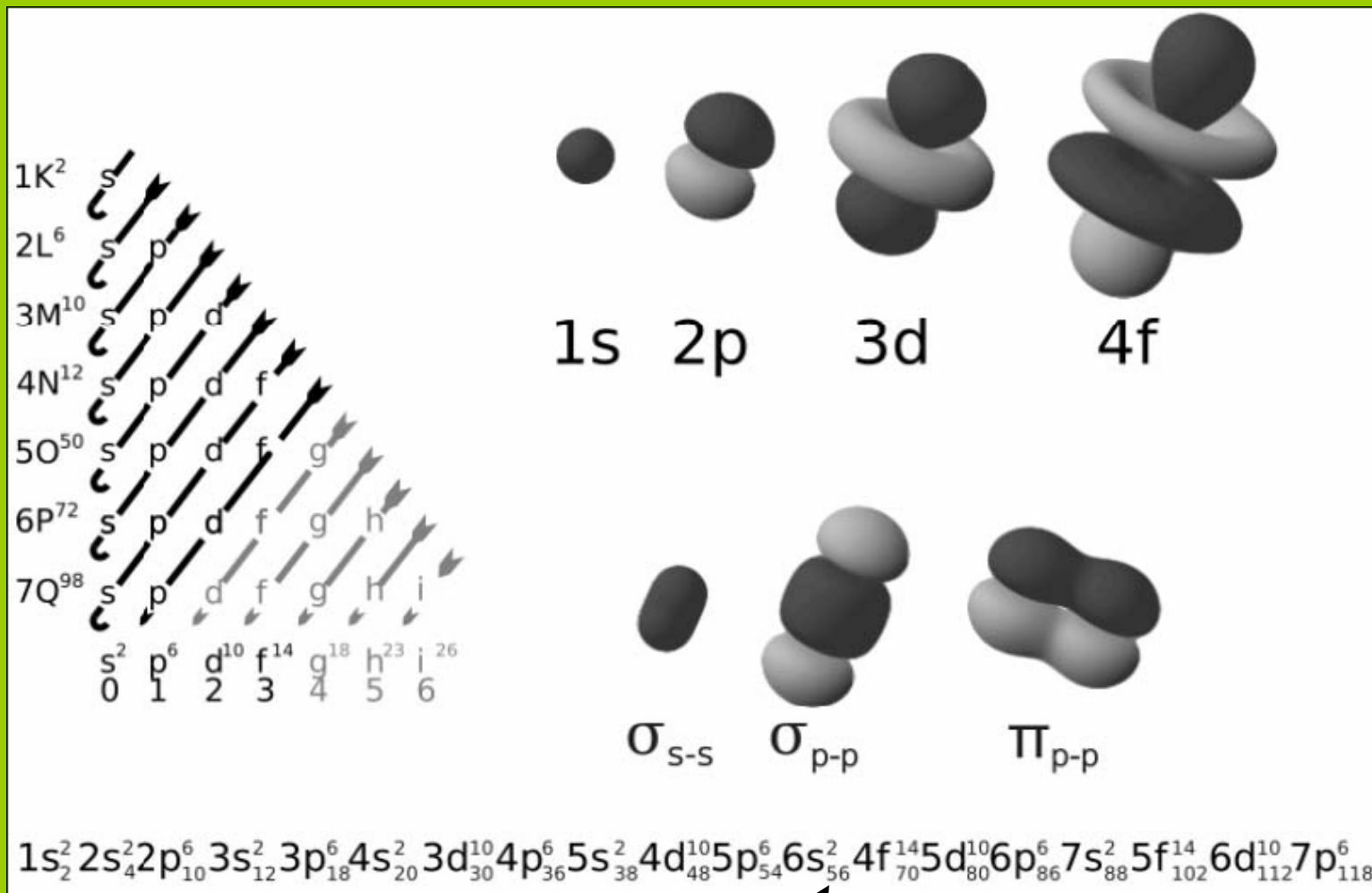
principio de Aufbau

subcapa 2p tres niveles energéticos, 2px, 2py, 2pz.

orbital **2p** hasta seis electrones,

un electrón en cada uno antes que alguno llegue a tener dos.





Columna de gases nobles

REGLA DEL SERRUCHO: 1s → 2s → 2p → 3s → 3p → 4s → 3d → 4p → 5s -----

Configuraciones atómicas p^n y d^n

p^1 : 2P

p^2 : $^1S, ^1D, ^3P$

p^3 : $^2P, ^2D, ^4S$

p^4 : $^1S, ^1D, ^3P$

p^5 : 2P

d^1, d^9 : 2D

d^2, d^8 : $^1S, ^1D, ^1G, ^3P, ^3F$

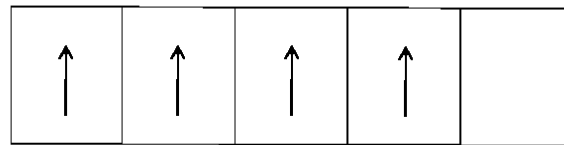
d^3, d^7 : $^2P, ^2D$ (twice), $^2F, ^2G, ^2H, ^4P, ^4F$

d^4, d^6 : 1S (twice), 1D (twice), $^1F, ^1G$ (twice), $^1I, ^3P$ (twice)

$^3D, ^3F$ (twice), $^3G, ^3H, ^5D$

d^5 : $^2S, ^2P, ^2D$ (three times), 2F (twice), 2G (twice),

$^2H, ^2I, ^4P, ^4D, ^4F, ^4G, ^6S$



m_l 2 1 0 -1 -2

Microestado d^4 ; $M_l=2$,
 $M_s=2$



$2S + 1$	Name	$2S + 1$	Name
1	Singlet	6	Sextet
2	Doublet	7	Septet
3	Triplet	8	Octet
4	Quartet	9	Nonet
5	Quintet	10	Decet

$$\begin{aligned} \langle H_{\text{so}} \rangle &= \zeta \langle \mathbf{L} \cdot \mathbf{S} \rangle = \zeta \langle nJM_JLS | \mathbf{L} \cdot \mathbf{S} | nJM_JLS \rangle \\ &= \frac{\zeta [J(J+1) - L(L+1) - S(S+1)]}{2}. \end{aligned}$$

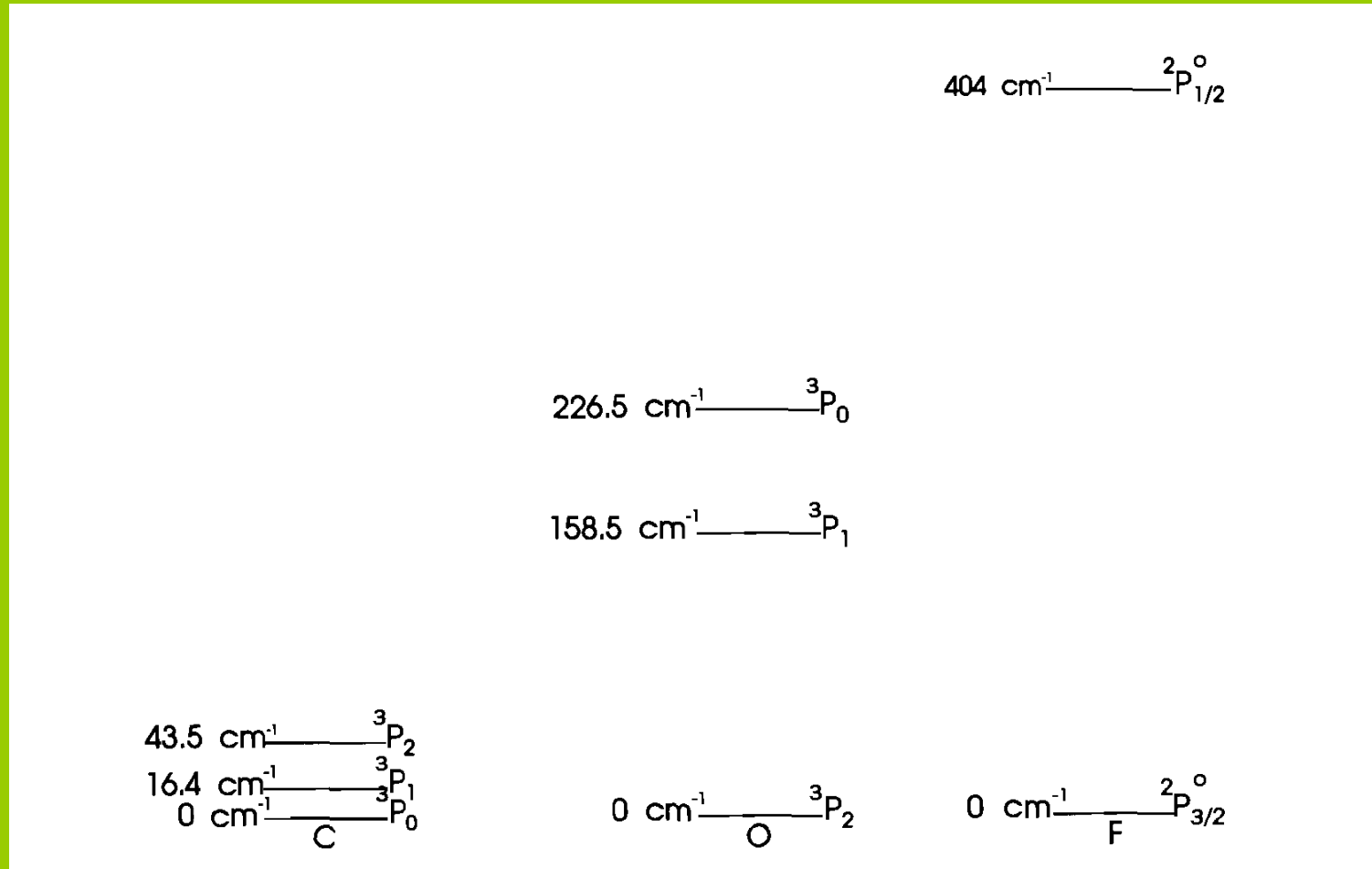
$$E_{J+1} - E_J = \frac{\zeta [(J+1)(J+2) - J(J+1)]}{2} = \zeta(J+1).$$

Intervalo de Landé



Valores permitidos de J: L+S, L+S-1, | L-S|

Splitting de los multipletes mas bajos de C, O, F (Landé)



C: $1s^2, 2s^2, 2p^2$

O: $1s^2, 2s^2, 2p^4$

F: $1s^2, 2s^2, 2p^5$

$2S+1L_J$

Efecto Zeeman

$$\boldsymbol{\mu}_L = \gamma \mathbf{L}.$$

$$|\mathbf{L}| = [L(L + 1)]^{1/2} \hbar$$

$$|\boldsymbol{\mu}_L| = -\left(\frac{e\hbar}{2m_e}\right) \sqrt{L(L + 1)} = -\mu_B \sqrt{L(L + 1)},$$

$$\boldsymbol{\mu}_S = g_e \gamma \mathbf{S} = g_e \left(\frac{-\mu_B}{\hbar}\right) \mathbf{S},$$

$$g_e = 2.0023$$

Campo \mathbf{B} externo

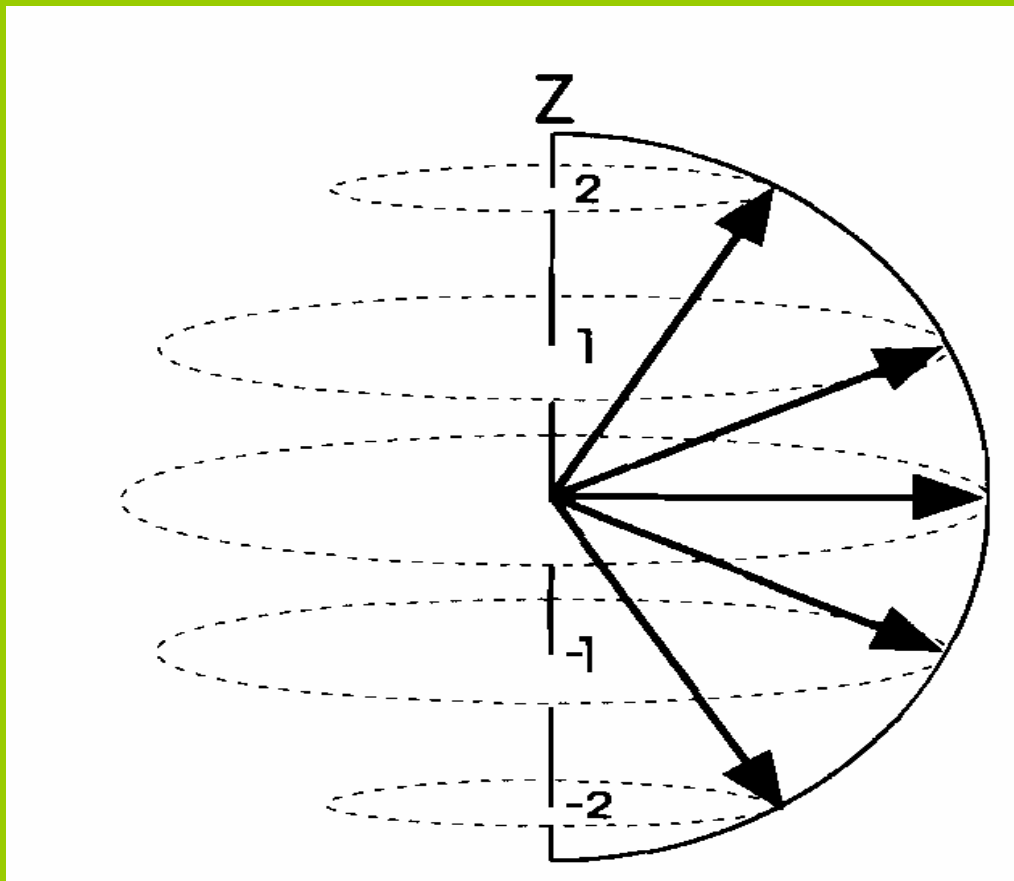
$$\hat{H}' = -\boldsymbol{\mu} \cdot \mathbf{B}$$

Momento magnético nuclear:

$$\boldsymbol{\mu}_I = \gamma_I \mathbf{I} = g_I \frac{\mu_N}{\hbar} \mathbf{I}$$

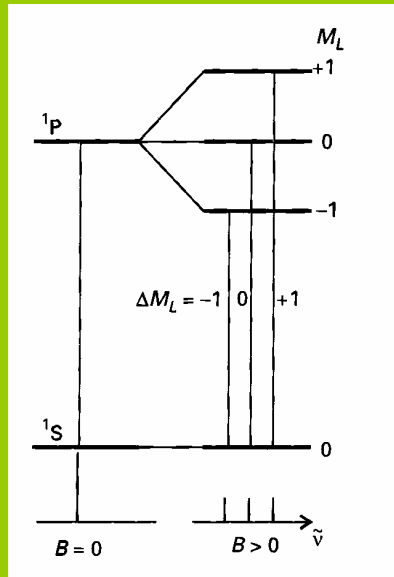
$$\mu_N = \frac{e\hbar}{2m_p}$$

$$\nu = \frac{\Delta(\boldsymbol{\mu} \cdot \mathbf{B})}{\hbar}$$



**ZEEMAN normal (singletes)
para sistema de muchos electrones**

$$H^{(1)} = -m_z \mathcal{B} = -\gamma_e (l_{z1} + l_{z2} + \dots) \mathcal{B} = -\gamma_e L_z \mathcal{B}$$



$${}^1P \rightarrow {}^1S$$

Intervalo: $\mu_L B$
Independiente de L

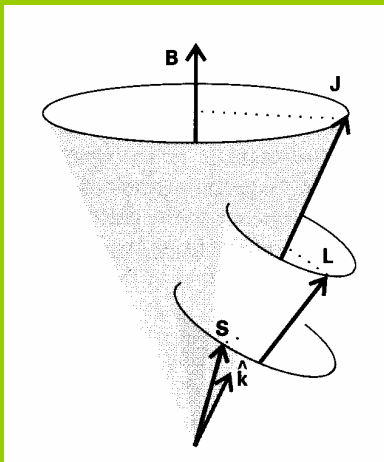
$$\Delta M_L = \pm 1$$

Luz polarizada perpend a **B**

$$\Delta M_L = 0$$

Luz polarizada paralela a **B**

EFEECTO ZEEMAN ANOMALO



$$H^{(1)} = -\mathbf{m}_{\text{orbital}} \cdot \mathbf{B} - \mathbf{m}_{\text{spin}} \cdot \mathbf{B} = -\gamma_e (\mathbf{L} + 2\mathbf{S}) \cdot \mathbf{B}$$

(el momento de spin es no nulo)

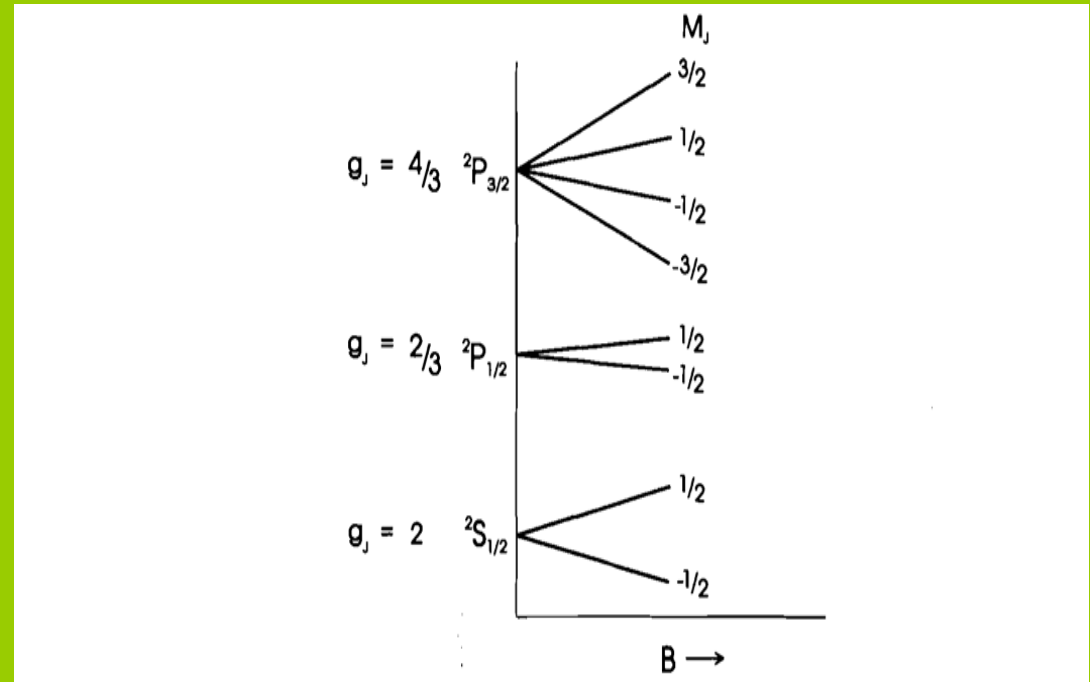
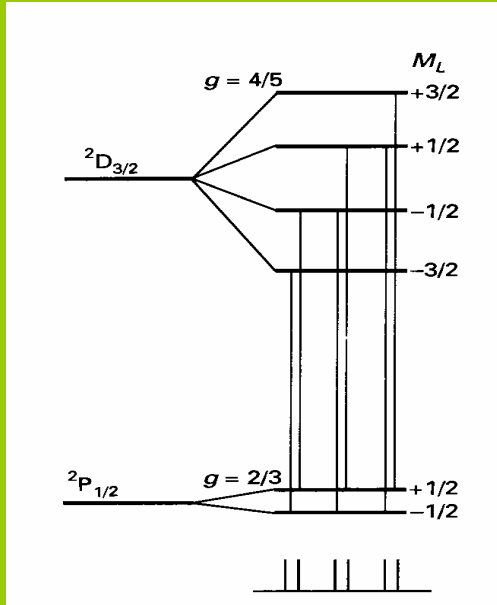
$$\begin{aligned}\boldsymbol{\mu}_J &= \left[\boldsymbol{\mu}_S \cdot \frac{\mathbf{J}}{|\mathbf{J}|^2} + \frac{\boldsymbol{\mu}_L \cdot \mathbf{J}}{|\mathbf{J}|^2} \right] \mathbf{J} \\ &= \left[\gamma(g_s \mathbf{S} + \mathbf{L}) \cdot \frac{\mathbf{J}}{|\mathbf{J}|^2} \right] \mathbf{J},\end{aligned}$$

$$H^{(1)} = -g_J \gamma_e \mathbf{J} \cdot \mathbf{B}$$

$$\begin{aligned}H^{(1)} &= -\gamma_e (\mathbf{L} + 2\mathbf{S}) \cdot \mathbf{B} \\ &= -\gamma_e \left\{ 1 + \frac{J(J+1) + S(S+1) - L(L+1)}{2J(J+1)} \right\} \mathbf{J} \cdot \mathbf{B}\end{aligned}$$

Zeeman normal

Zeeman para los primeros 3 estados de un alcalino



$$\nu_L = \frac{\mu_B B}{h}$$

$$E_{M_J} = \langle \hat{H}' \rangle = -\langle \mu_J \cdot \mathbf{B} \rangle = g_J \frac{\mu_B}{\hbar} \langle \mathbf{J} \cdot \mathbf{B} \rangle = g_J \frac{\mu_B B}{\hbar} \langle J_z B_z \rangle = g_J \mu_B M_J B,$$

Estructura hiperfina

Momento de spin nuclear \mathbf{I}

$$\mathbf{F} = \mathbf{J} + \mathbf{I}.$$

$$H_{\text{hf}} = \left(\frac{\mu_0 g_e \gamma_e \gamma_N}{4\pi r^3} \right) \left(\mathbf{s} \cdot \mathbf{I} - \frac{3(\mathbf{s} \cdot \mathbf{r})(\mathbf{r} \cdot \mathbf{I})}{r^2} \right)$$

Interacción
entre momentos
magnéticos

$$H_{\text{hf}} = -\frac{2}{3} g_e \gamma_e \gamma_N \mu_0 \delta(\mathbf{r}_N) \mathbf{s} \cdot \mathbf{I}$$

Contacto de
Fermi

Acoplamiento entre
spines nucleares

$$H^{(\text{spin})} = J \mathbf{I}_A \cdot \mathbf{I}_B$$